

SFB 443

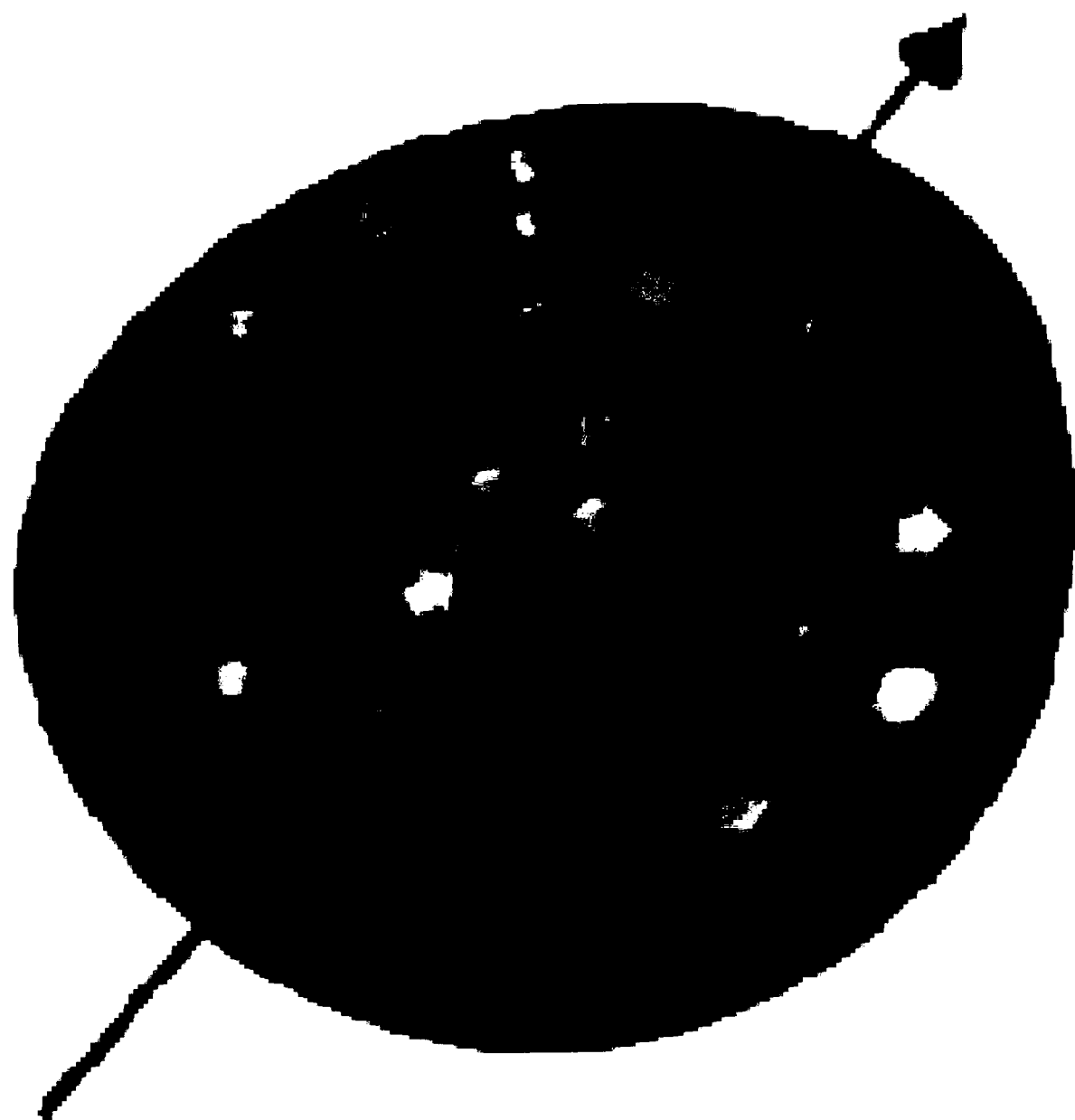
# Hadron Physics at the Mainz Microtron MAMI

Thomas Walcher

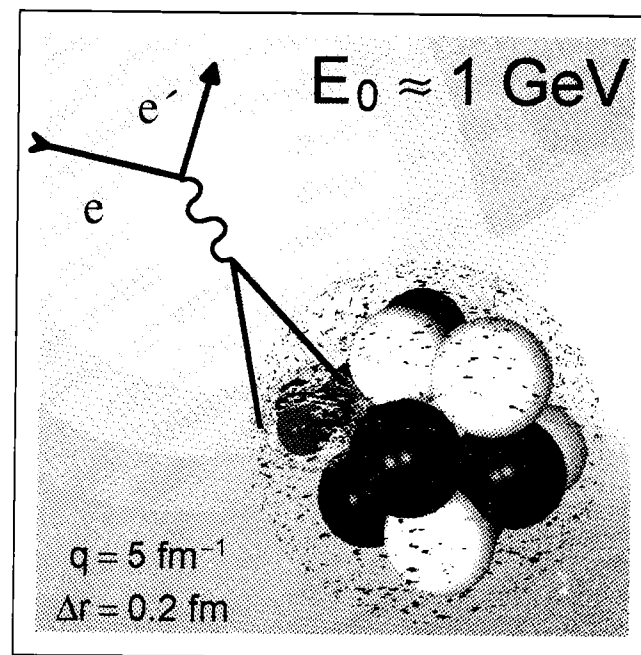
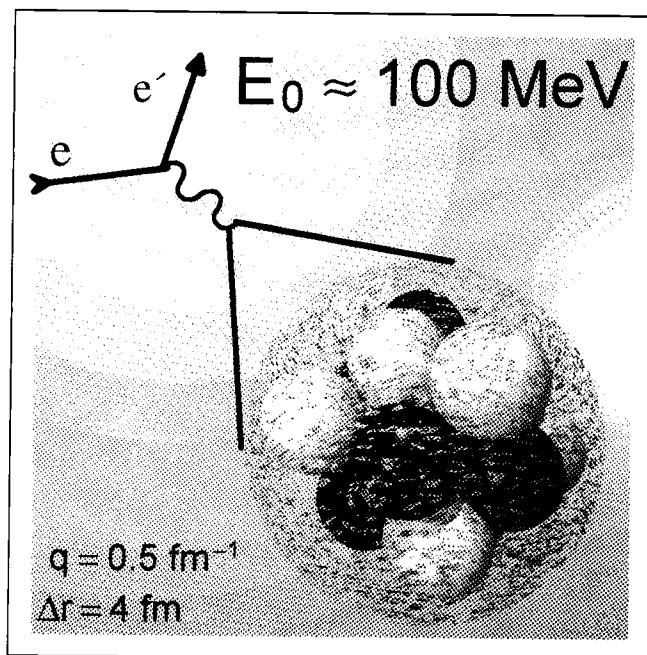
Institut für Kernphysik

Johannes Gutenberg-Universität Mainz, Germany

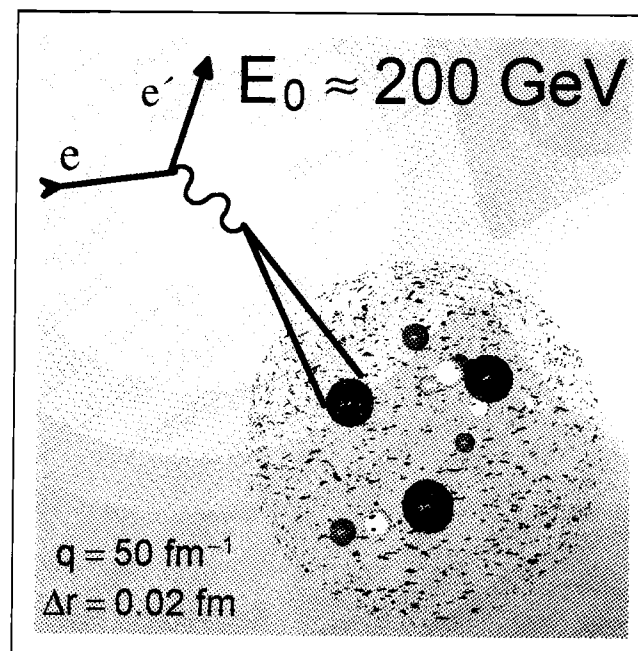
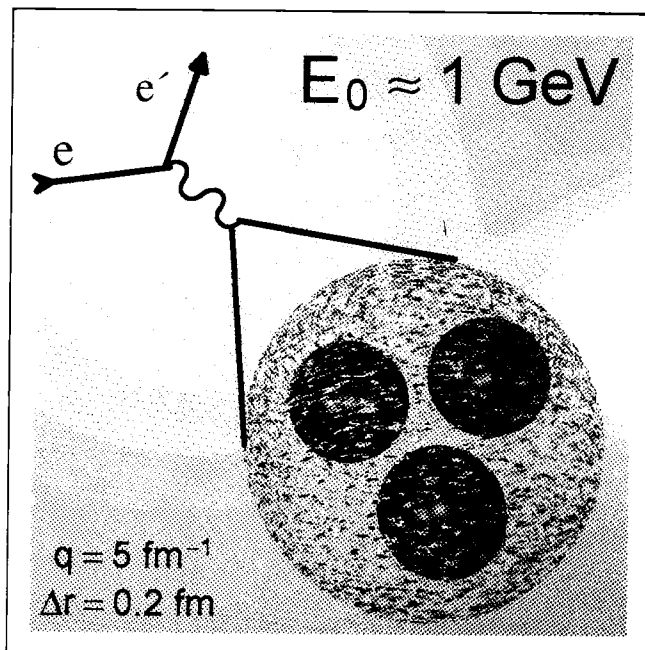
1. Introduction: Why and how hadron physics?
  2. Recent highlights of MAMI
    - Form factors of the nucleon
    - Pion polarizability
  3. MAMI C
    - Energy increase to 1500 MeV: MAMI C
    - CB@MAMI
    - KAOS@MAMI
  4. Extended opportunities at MAMI C
    - overview
    - nucleon resonances in selective decay channels
  5. Conclusions
-



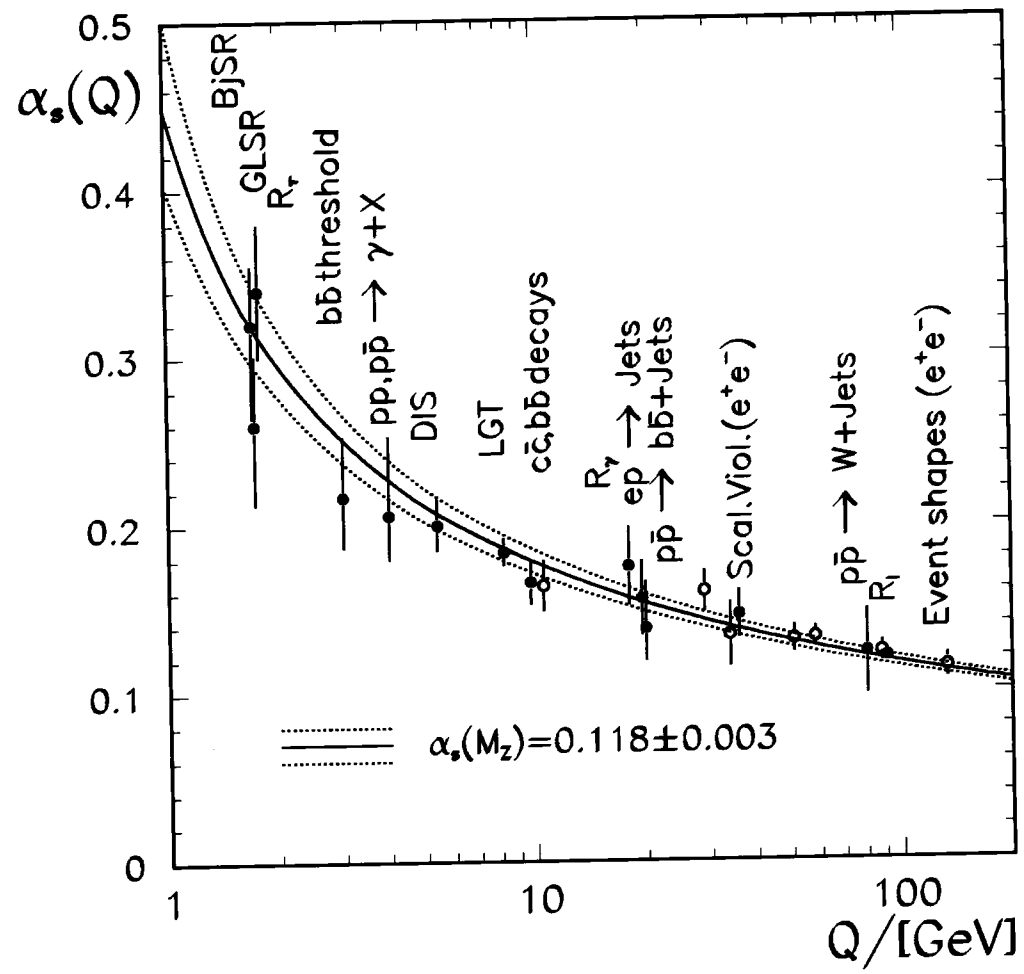
# Nucleus

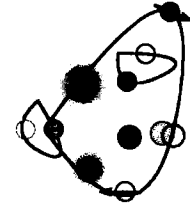


# Nucleon



running coupling constant of the strong interaction



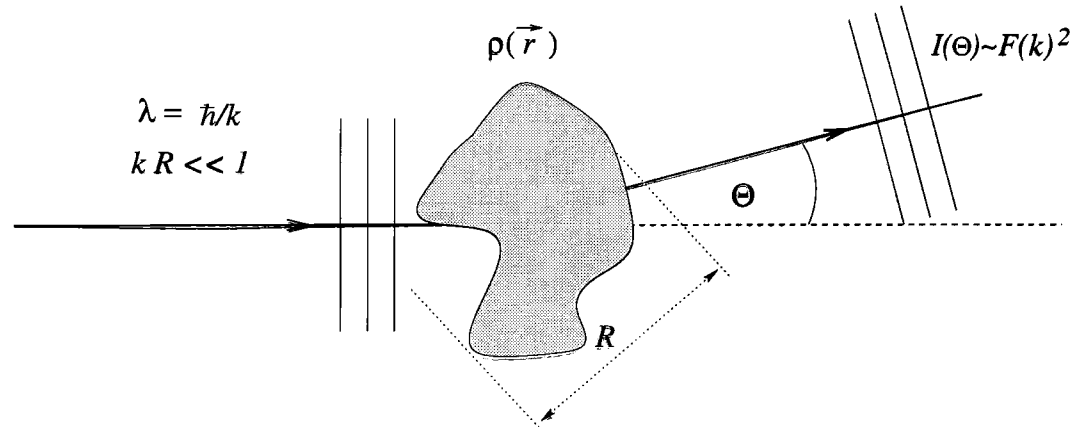


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Form factors of the nucleon

# Elastic Formfactors

scattering of light:



$$I(\Theta) = I_0 \cdot \left( \frac{d\sigma}{d\Omega} \right)_{Thompson} \cdot |F(\vec{k})|^2$$

$$F(\vec{k}) \equiv \int (\rho(\vec{r}) \cdot e^{i\vec{k} \cdot \vec{r}}) d^3\vec{r}$$

elastic electron-nucleon-scattering:

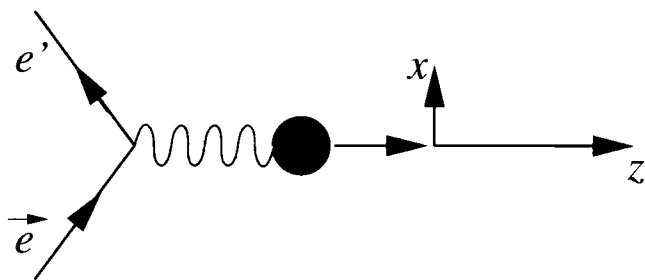
$$\frac{d\sigma}{d\Omega} = \left( \frac{d\sigma}{d\Omega} \right)_{Mott} \cdot \left( \frac{G_E^2(Q^2) + \tau G_M^2(Q^2)}{1 + \tau} + 2\tau G_M^2(Q^2) \tan^2 \frac{\Theta}{2} \right)$$

$$Q^2 = \vec{q}^2 - \omega^2; \quad \tau \equiv Q^2/4M^2$$

4 formfactors :  $G_{E,p}(Q^2), G_{M,p}(Q^2)$

$$G_{E,n}(Q^2), G_{M,n}(Q^2)$$

# Measurement of $G_{E,n}$ in $D(\vec{e}, e'\vec{n})p$



LD<sub>2</sub> Target

Dipole  
Magnet

Front Wall

Rear Wall

$$\text{Asymmetry } A = P_e \mathcal{A}_{\text{eff}} P_t \sin \Phi_n$$

$$P_x = -hP_e \frac{aG_E G_M}{G_E^2 + bG_M^2}$$

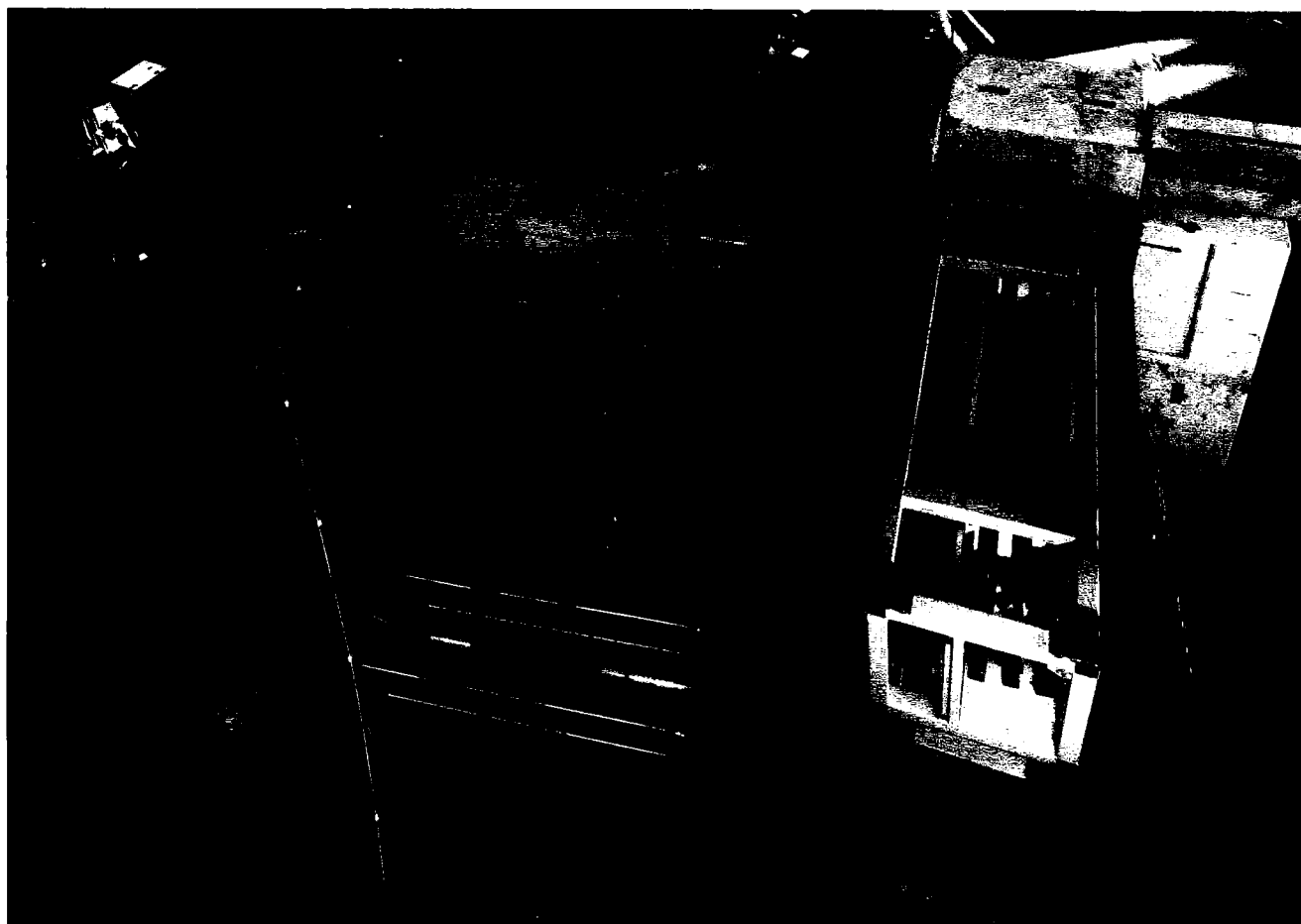
$$P_y = 0$$

$$P_z = hP_e \frac{cG_M^2}{G_E^2 + bG_M^2}$$

Arnold, Carlson & Gross,  
PR C **23** (1981), 363

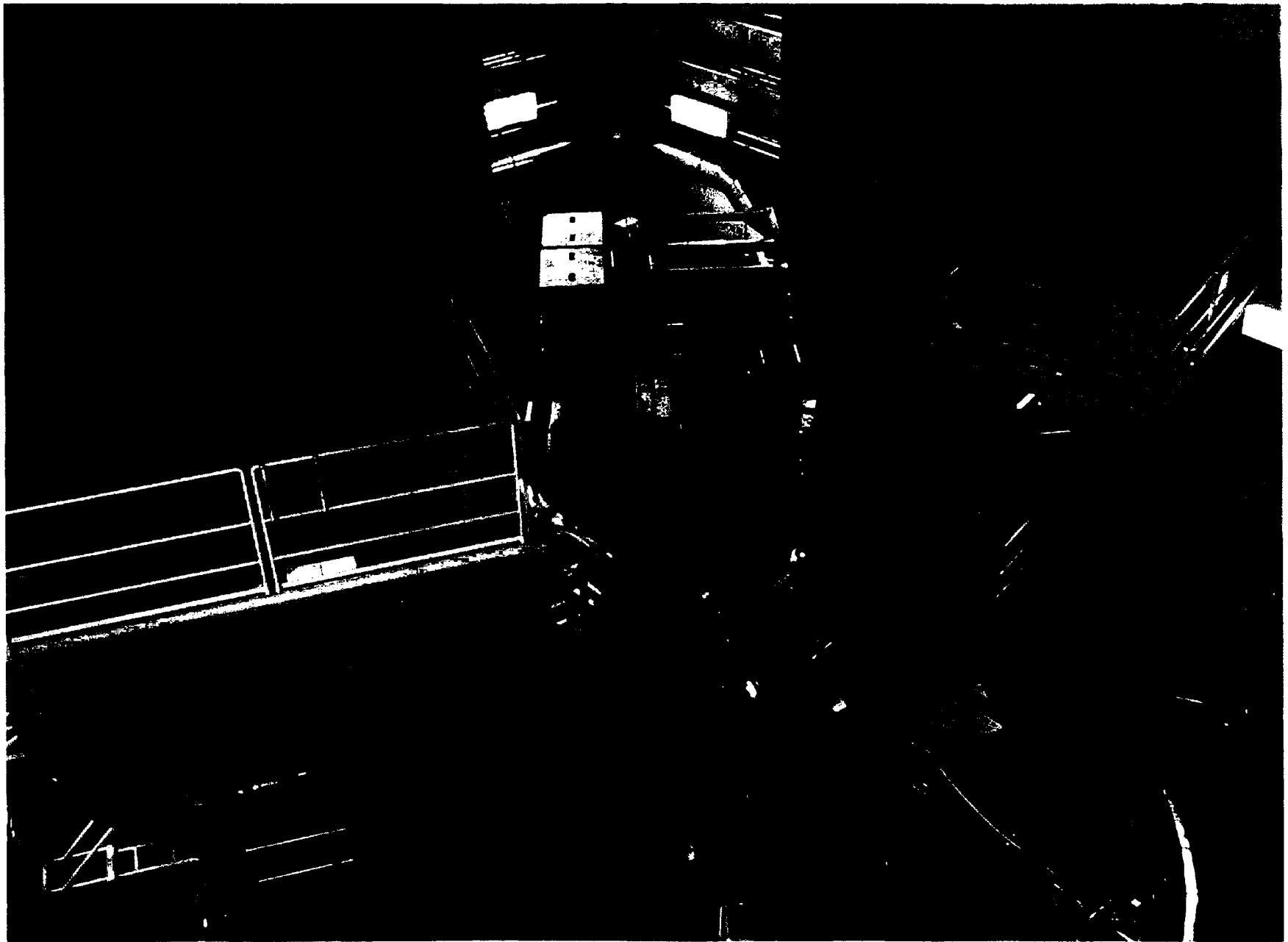
Method:

T. N. Taddeucci et al.,  
NIM **A241** (1985), 448



Michael Seimetz

# A1 Three Spectrometer Setup



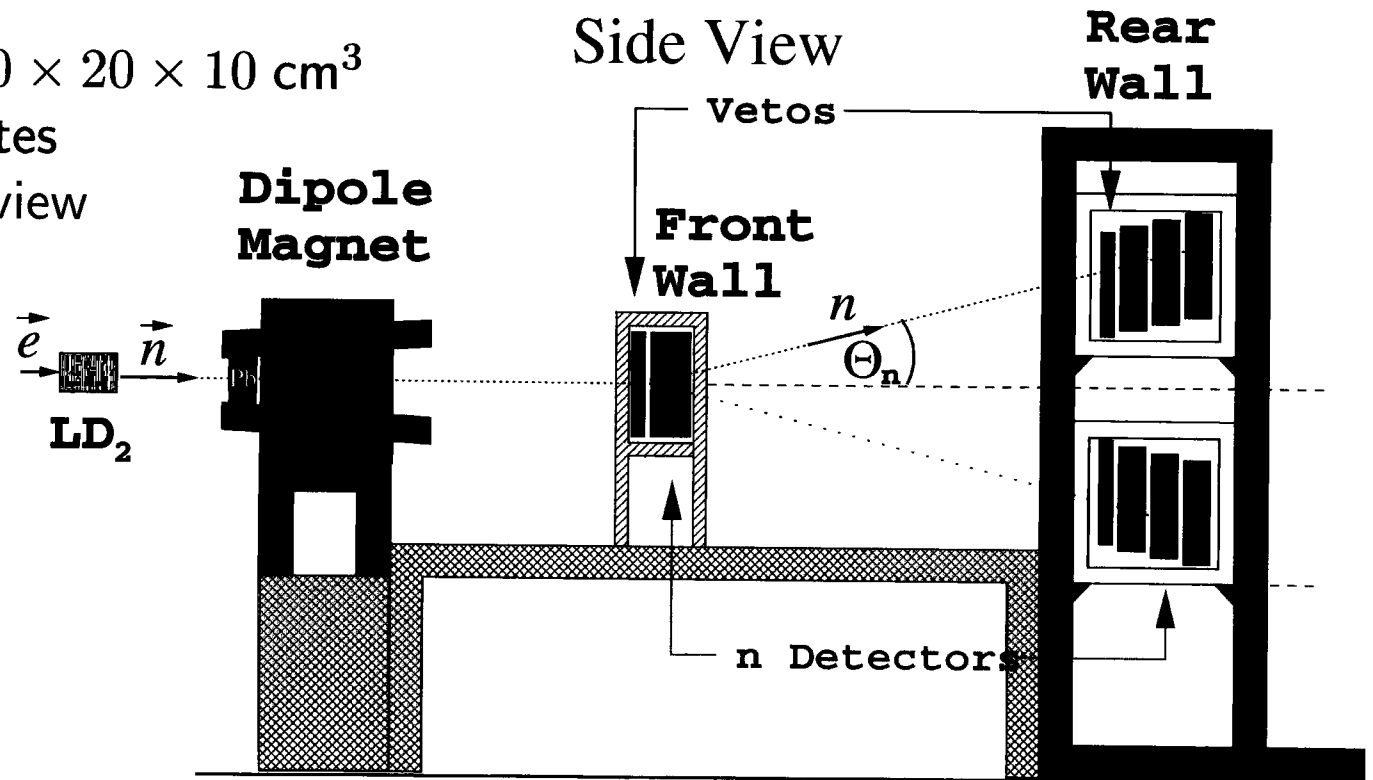
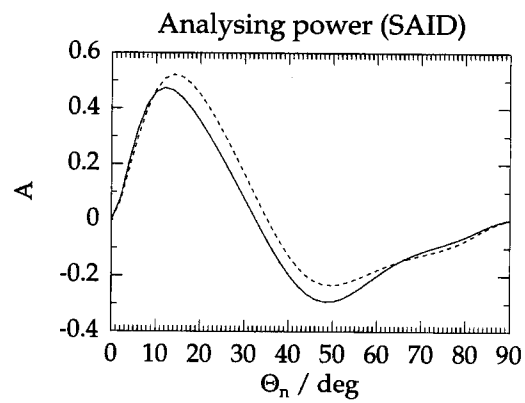


## Neutron Polarimeter, Rear Wall

24 scintillator bars,  $180 \times 20 \times 10 \text{ cm}^3$

⇒ high background rates

⇒ avoid direct target view



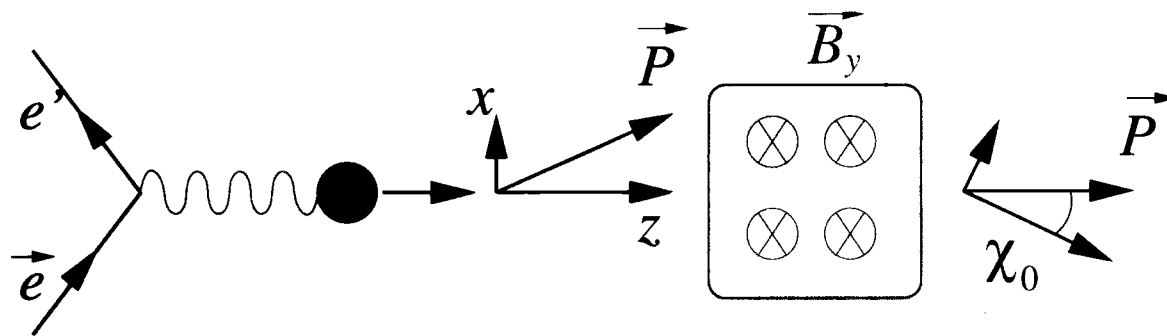
Measurement of  $G_{E,n}$  in  $D(\vec{e}, e'\vec{n})p$

## Spin Precession Method

Mixing of two spin components by precession of neutron spin in magnetic field,

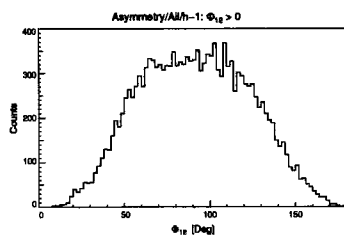
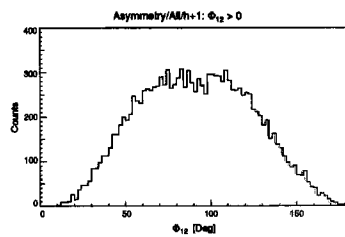
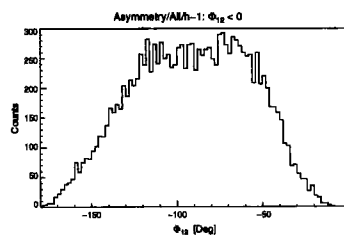
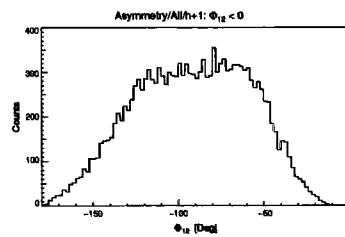
$$\mathcal{P}_t(\chi) = \mathcal{P}_x \cos(\chi) + \mathcal{P}_z \sin(\chi) =: \mathcal{P}_0 \sin(\chi - \chi_0)$$

(M. Ostrick et al., PRL **83** (1999) 276)



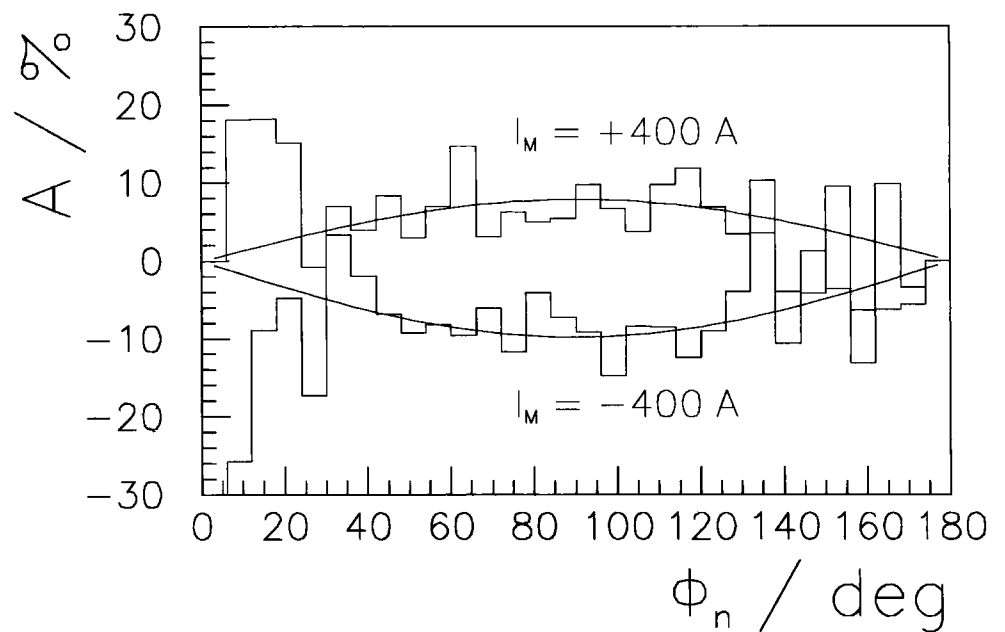
$$\tan \chi_0 = \frac{\mathcal{P}_x}{\mathcal{P}_z} = \frac{A_x}{A_z} = \frac{a \mathcal{A}_{\text{eff}} P_e}{c \mathcal{A}_{\text{eff}} P_e} \cdot \frac{G_{E,n}}{G_{M,n}} .$$

## Asymmetries

 $\Phi_n$  distributions: $h = -1, \Phi_n > 0$  $h = +1, \Phi_n > 0$  $h = -1, \Phi_n < 0$  $h = +1, \Phi_n < 0$ 

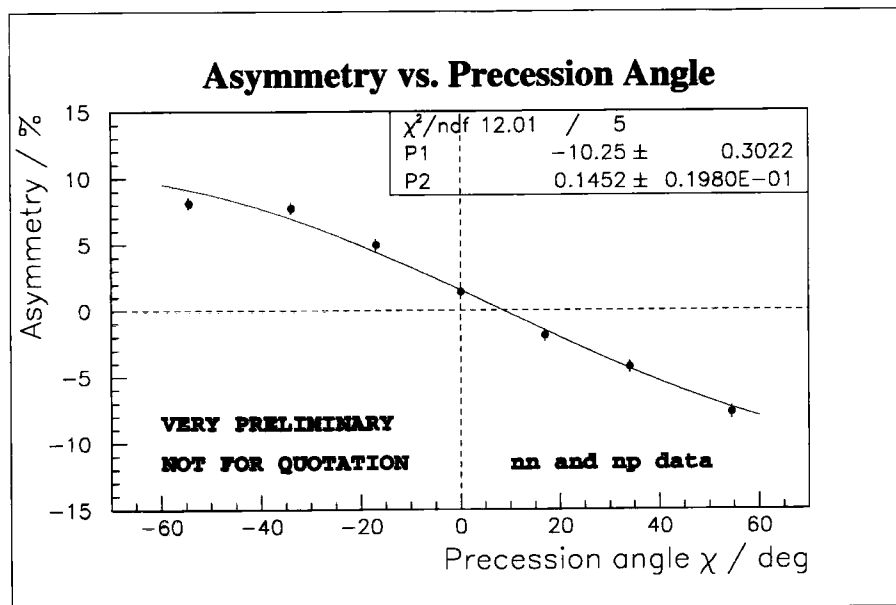
$$A(\Phi_n) = \frac{\sqrt{N^+(\Phi_n)N^-(\Phi_n+\pi)} - \sqrt{N^+(\Phi_n+\pi)N^-(\Phi_n)}}{\sqrt{N^+(\Phi_n)N^-(\Phi_n+\pi)} + \sqrt{N^+(\Phi_n+\pi)N^-(\Phi_n)}}$$

## Asymmetry



# Asymmetries

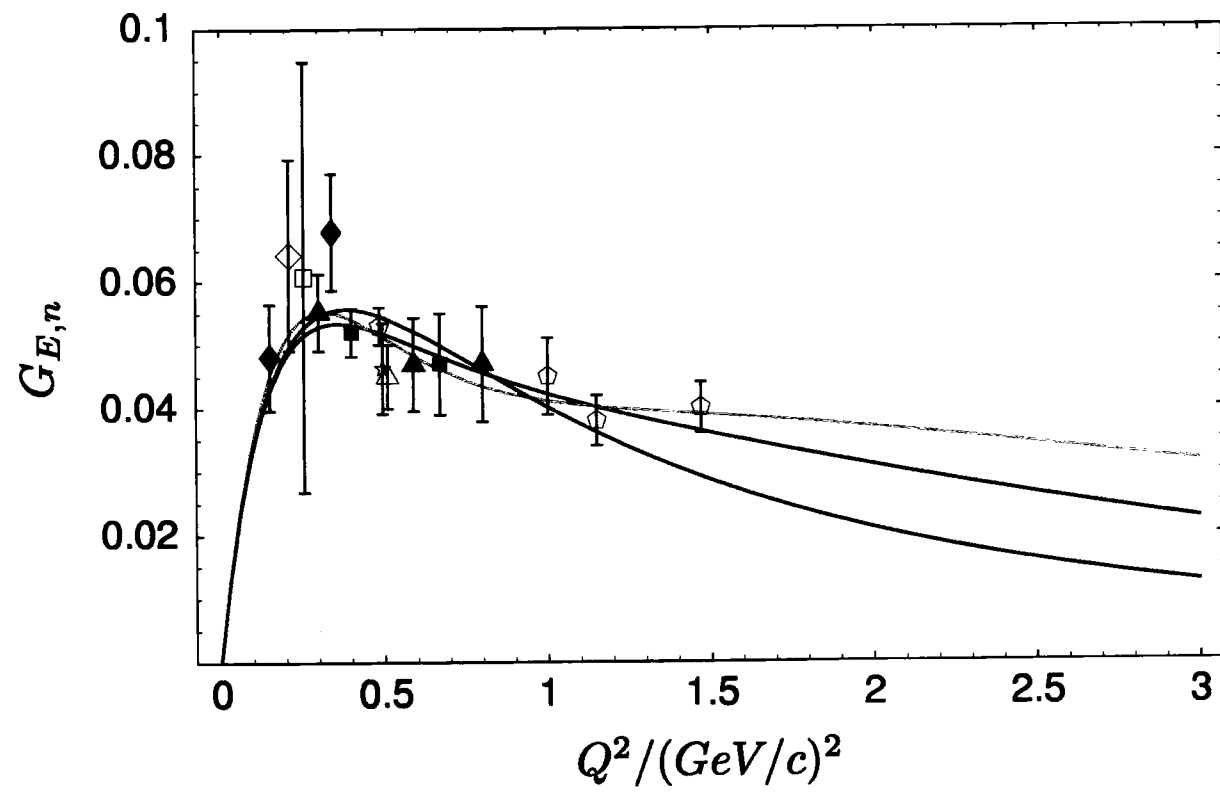
Plot asymmetries as function of spin precession angle  $\chi$



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electric form factor of the neutron

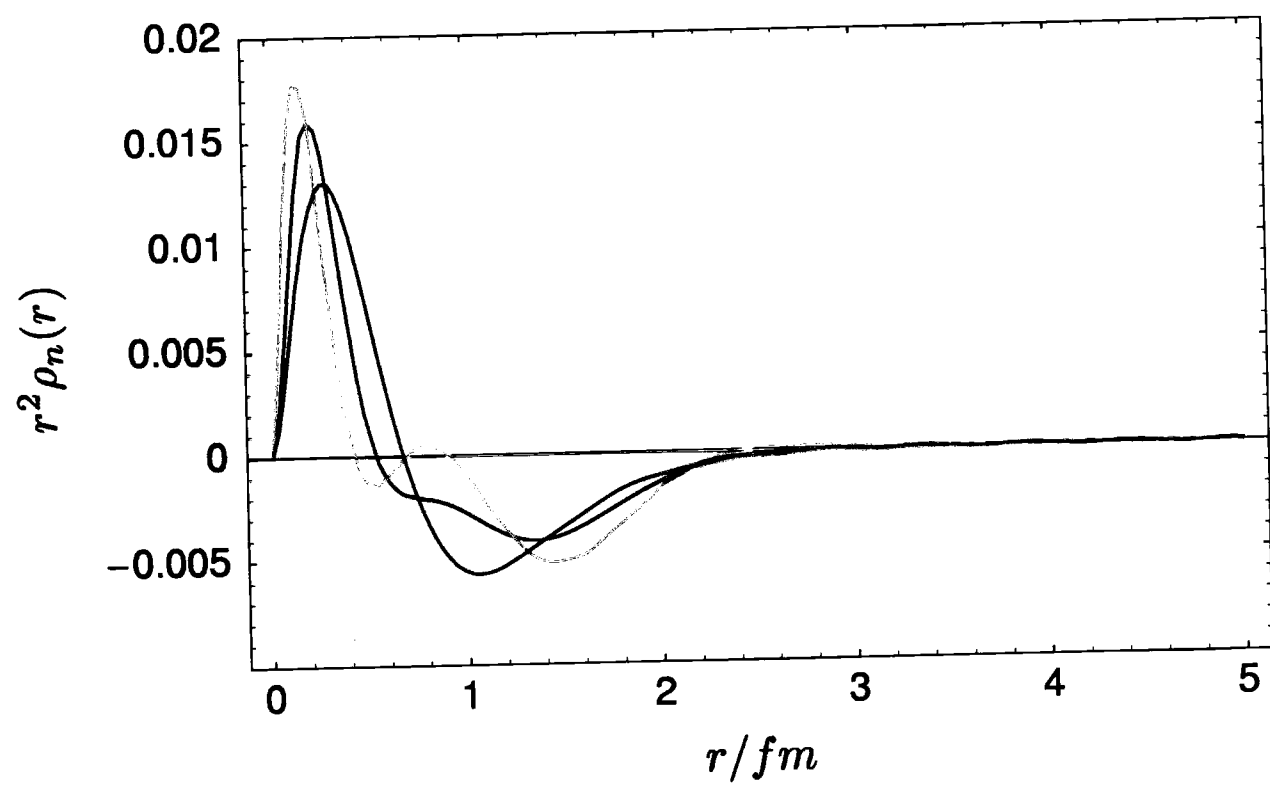
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electric charge distribution of the neutron

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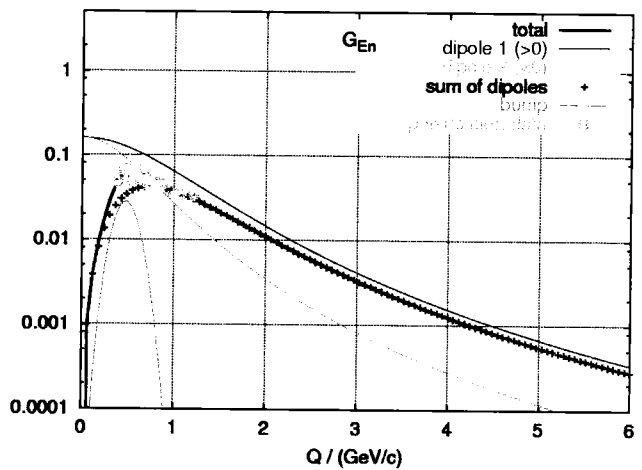
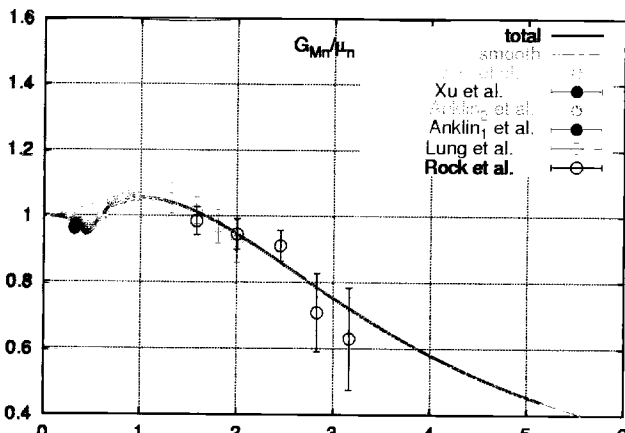
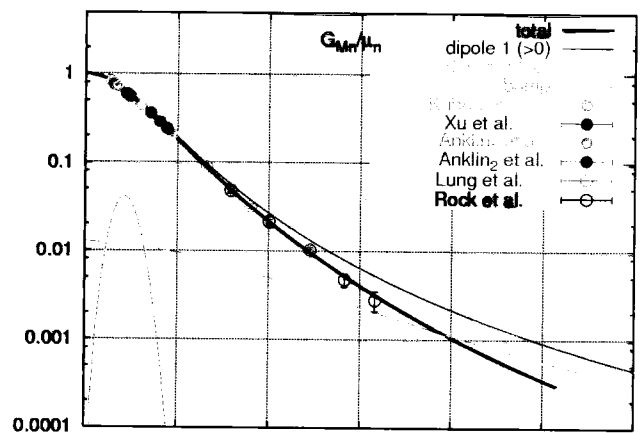
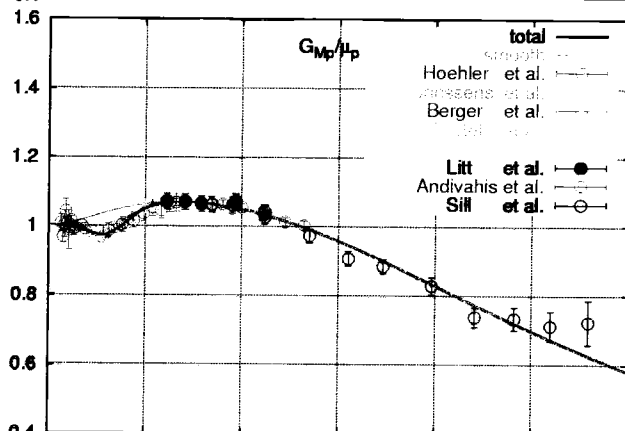
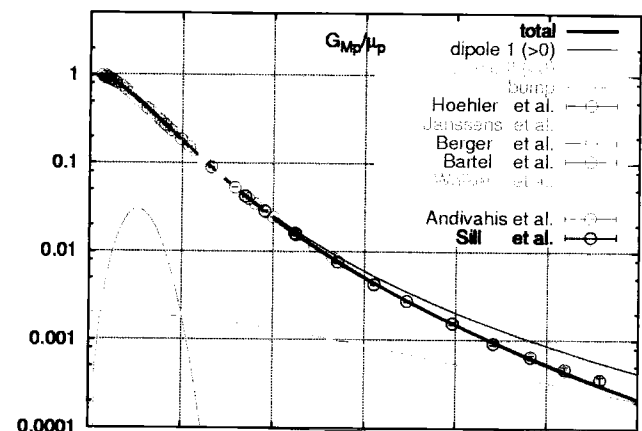
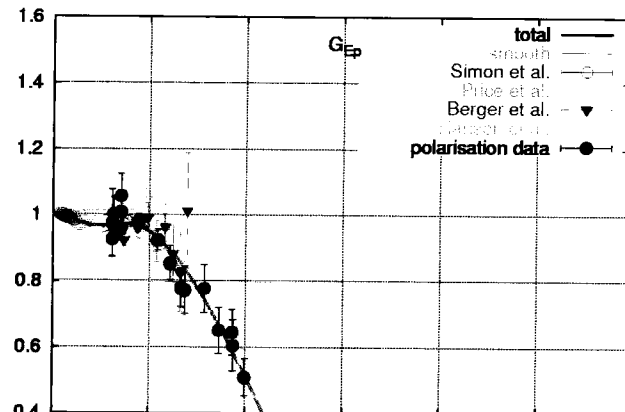
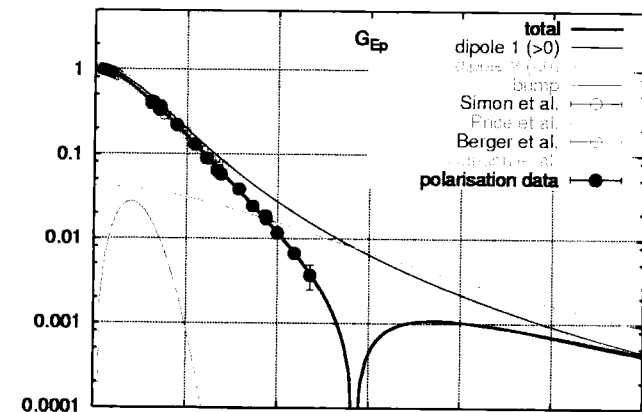


# Form factors of the nucleon

fit with 2 dipole shapes and 1 "Gauss"

form factors

form factor / standard dipole

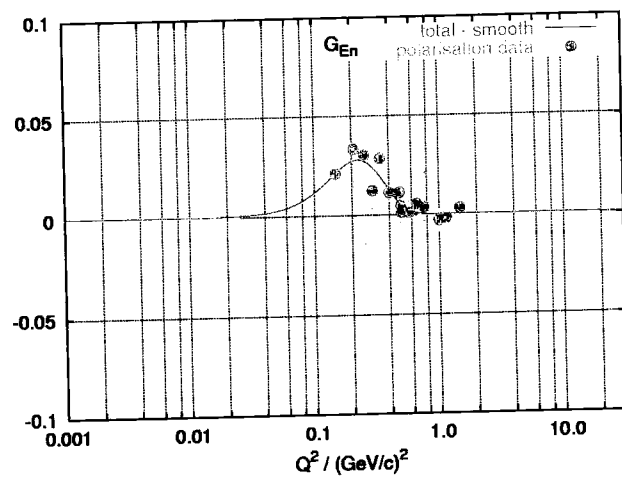
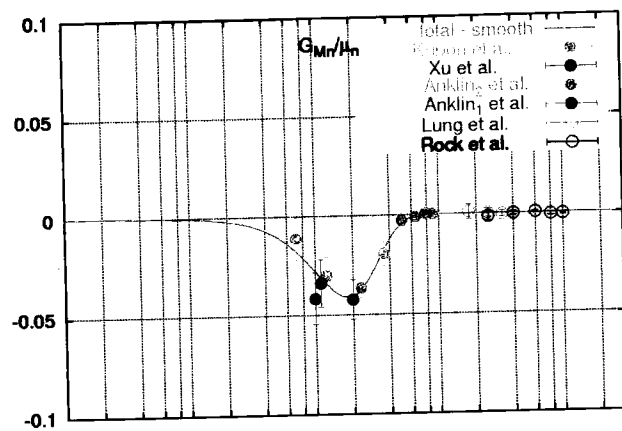
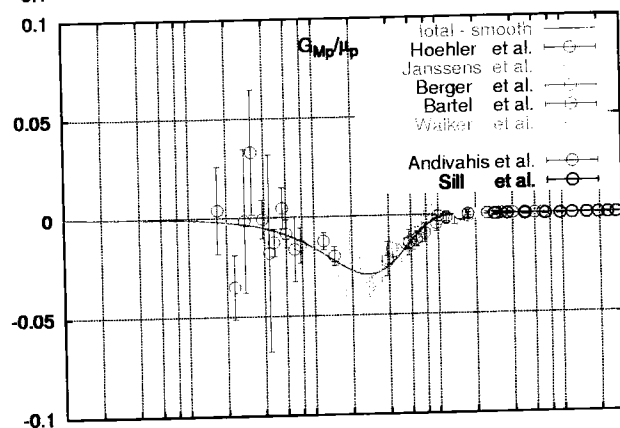
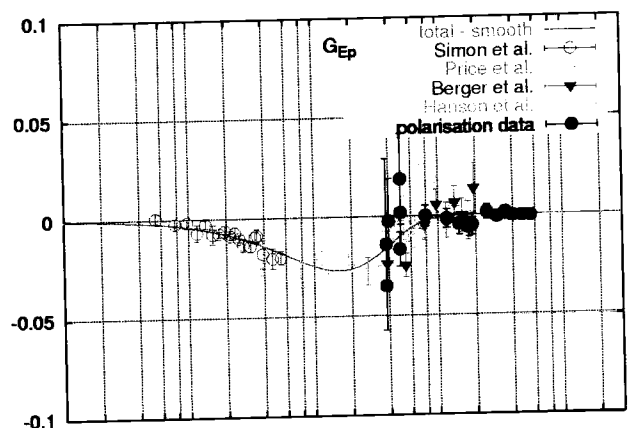


$Q / (\text{GeV}/c)$

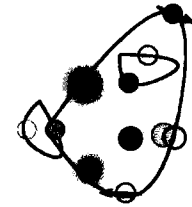
$Q / (\text{GeV}/c)$

# Form factors of the nucleon

measurement minus smooth fit  $\equiv$  2 dipole shapes plus "Gauss"







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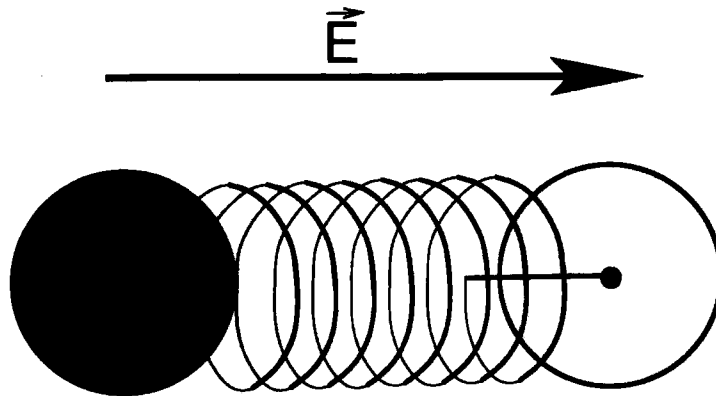
Measurement of the  $\pi^+$  polarizability in the  $\gamma p \rightarrow \gamma' \pi^+ n$  reaction.

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## Meaning of the polarizability of a composed system

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electric polarizability  $\alpha$



spring

$$\vec{p}_{el} := q\delta = q \frac{q}{D} \vec{E} =: \epsilon_0 \alpha \vec{E} \quad \leadsto \quad \alpha = \frac{1}{\epsilon_0} \frac{q^2}{D} = 4\pi \hbar c \alpha_{QED} \frac{\zeta^2}{D}; \quad D = \frac{G}{4} \frac{r^4}{R^3}$$

$$\alpha_{spring} = \hbar c \frac{\alpha_{QED}}{G} 16\pi \frac{R^3}{r^4} \zeta^2$$

$$\alpha_{spring} \propto \frac{\alpha_{QED}}{\alpha_{spring}} \text{length}^3$$

## Experimental situation

Experiments	$\alpha_{\pi^\pm}/10^{-4}\text{fm}^3$	$\alpha_{\pi^0}/10^{-4}\text{fm}^3$
$\pi^- Z \rightarrow \gamma\pi^- Z$ , Serpukhov (1983)	$6.8 \pm 1.4 \pm 1.2$	
$\gamma p \rightarrow \gamma\pi^+ n$ , Lebedev Phys.Inst. (1984)	$20 \pm 12$	
D. Babusci <i>et al.</i> (1992)		
$\gamma\gamma \rightarrow \pi^+\pi^-$ : PLUTO (1984)	$19.1 \pm 4.8 \pm 5.7$	
DM 1 (1986)	$17.2 \pm 4.6$	
DM 2 (1986)	$26.3 \pm 7.4$	
MARK II (1990)	$2.2 \pm 1.6$	
$\gamma\gamma \rightarrow \pi^0\pi^0$ : Crystal Ball (1990)		$\pm 0.69 \pm 0.11$
F. Donoghue, B. Holstein (1993)		
$\gamma\gamma \rightarrow \pi^+\pi^-$ : MARK II	$2.7 \pm ?$	
$\gamma\gamma \rightarrow \pi^0\pi^0$ : Crystal Ball		$-0.5 \pm ?$
	$(\alpha + \beta)_{\pi^0}/10^{-4}\text{fm}^3$	$(\alpha - \beta)_{\pi^0}/10^{-4}\text{fm}^3$
A. Kaloshin, V. Serebryakov (1994)		
$\gamma\gamma \rightarrow \pi^0\pi^0$ : Crystal Ball	$1.00 \pm 005$	$-0.6 \pm 1.8$
L. Fil'kov, V. Kashevarov (1999)		
$\gamma\gamma \rightarrow \pi^0\pi^0$ : Crystal Ball	$0.98 \pm 003$	$-1.6 \pm 2.2$

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## Theoretical predictions

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- **chiral perturbation theory**

- ★  $(\alpha + \beta)_{\pi^+} = 0$  in leading order  $O(p^4)$

- $(\alpha + \beta)_{\pi^+} = (0.3 \pm 0.1) \times 10^{-4} \text{fm}^3$  in order  $O(p^6)$

- ★  $(\alpha - \beta)_{\pi^+} \approx 5.4 \times 10^{-4} \text{fm}^3$  one loop (Bijens, Cornet, 1988; Danoghue, Holstein 1989; Belluci, Gasser, Sainio, 1994)

- $(\alpha - \beta)_{\pi^+} = (4.4 \pm 1.0) \times 10^{-4} \text{fm}^3$  two loops (Bürigi, 1997)

- **Nambu-Jona-Lasino model**

- $\alpha = -\beta = (3.0 \pm 0.6) \times 10^{-4} \text{fm}^3$ ;  $(\alpha - \beta)_{\pi^+} = (6.0 \pm 0.8) \times 10^{-4} \text{fm}^3$

- **Dispersion relations**

- $(\alpha - \beta)_{\pi^+} = (10.3 \pm 1.9) \times 10^{-4} \text{fm}^3$  (Lev Fil'kov, Kashevarov, 1999)

- **non linear  $\sigma$  model**

- $(\alpha - \beta)_{\pi^+} = 20 \times 10^{-4} \text{fm}^3$  (Bernard, Hiller, Weise, 1988)

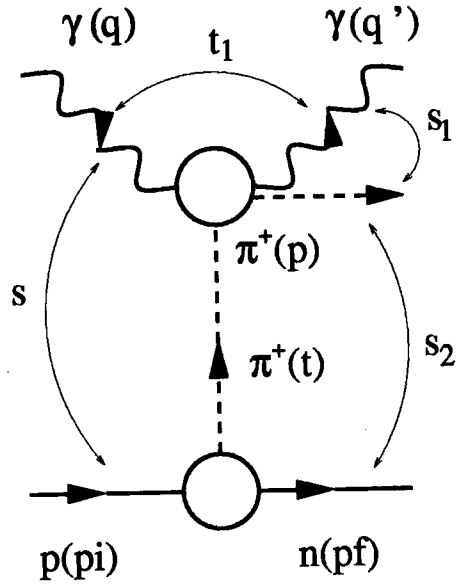
- **Dubna quark confinement model**

- $(\alpha - \beta)_{\pi^+} = 7.05 \times 10^{-4} \text{fm}^3$  (Ivanov, Mizutani, 1992)

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Basic idea for measuring the  $\pi^+$  polarizability.

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$$s = (p_1 + k_1)^2 = m_p^2 + 2m_p E_\gamma$$

$$t = (p_2 - p_1)^2 = (m_n - m_p)^2 - 2m_p(E_n - m_n)$$

$$t_1 = (k_2 - k_1)^2 = -2E_\gamma E_{\gamma'}(1 - \cos\theta_{\gamma\gamma'})$$

$$s_1 = (k_2 + q_2)^2 = m_\pi^2 + 2E_\gamma(q_{20} - |\vec{q}_2| \cos\theta_{\gamma\pi^+})$$

$$s_2 = (p_2 + q_2)^2 = s + t_1 - 2m_p E_\gamma$$

$$z = \cos\theta_{\gamma\gamma'}^{cm}$$

$$\frac{d\sigma_{\gamma\pi}}{d\Omega} = \left( \frac{d\sigma_{\gamma\pi}}{d\Omega} \right)_B - \frac{e^2 m_\pi^3 (s_1 - m_\pi^2)^2}{4\pi 4s_1^2 [(s_1 + m_\pi^2) + (s_1 - m_\pi^2)z]} \times \left\{ (1-z)^2 (\alpha_{\pi^\pm} - \beta_{\pi^\pm}) + \frac{s_1^2}{m_\pi^4} (1+z)^2 (\alpha_{\pi^\pm} + \beta_{\pi^\pm}) \right\}$$

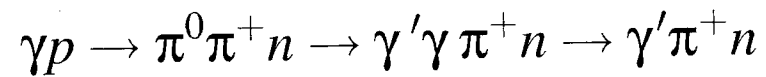
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## background reaction

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only backward direction of  $\gamma$  detection is interesting and covered (TAPS)

↪ background

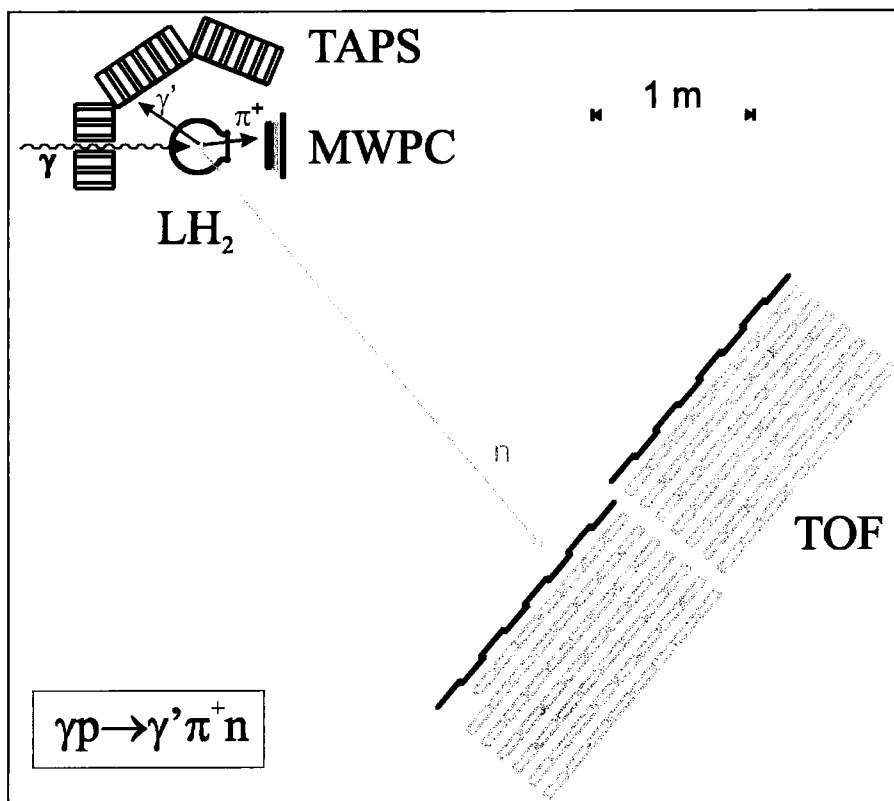


↓

lost

choice of detector setup suppresses this abundant reaction,  
Monte Carlo simulations show that with analysis methods:

- optimized cut ↪ background  $\leq 3\%$
- constrained fits ↪ background  $\leq 10\%$



TAPS:

A: 192 BaF2,  $\theta=68^\circ$

B: 192 BaF2,  $\theta=124^\circ$

C: 144 BaF2,  $\theta=180^\circ$

MWPC:

4 planes  $\times$  128 wires,  $\theta=0^\circ$

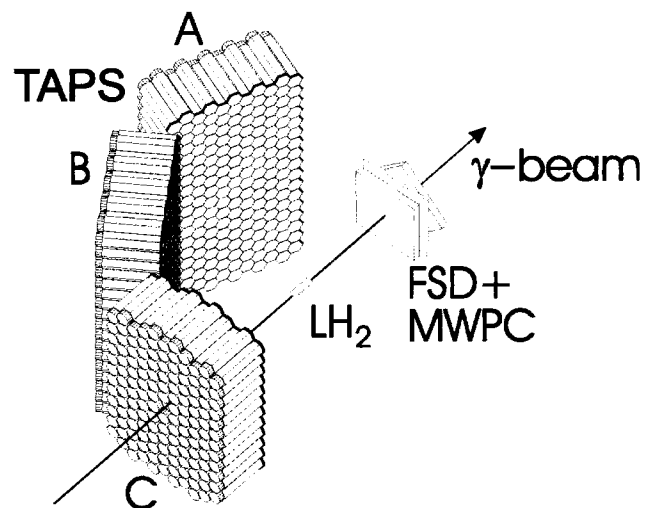
TOF:

111 bars,  $300 \times 20 \times 5 \text{ cm}^3$ ,  $\theta=40^\circ$

16 veto bars  $300 \times 22 \times 1 \text{ cm}^3$

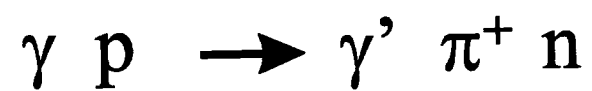
Target:

LH<sub>2</sub>, 11 cm long, 3 cm dia.





# Differential cross section

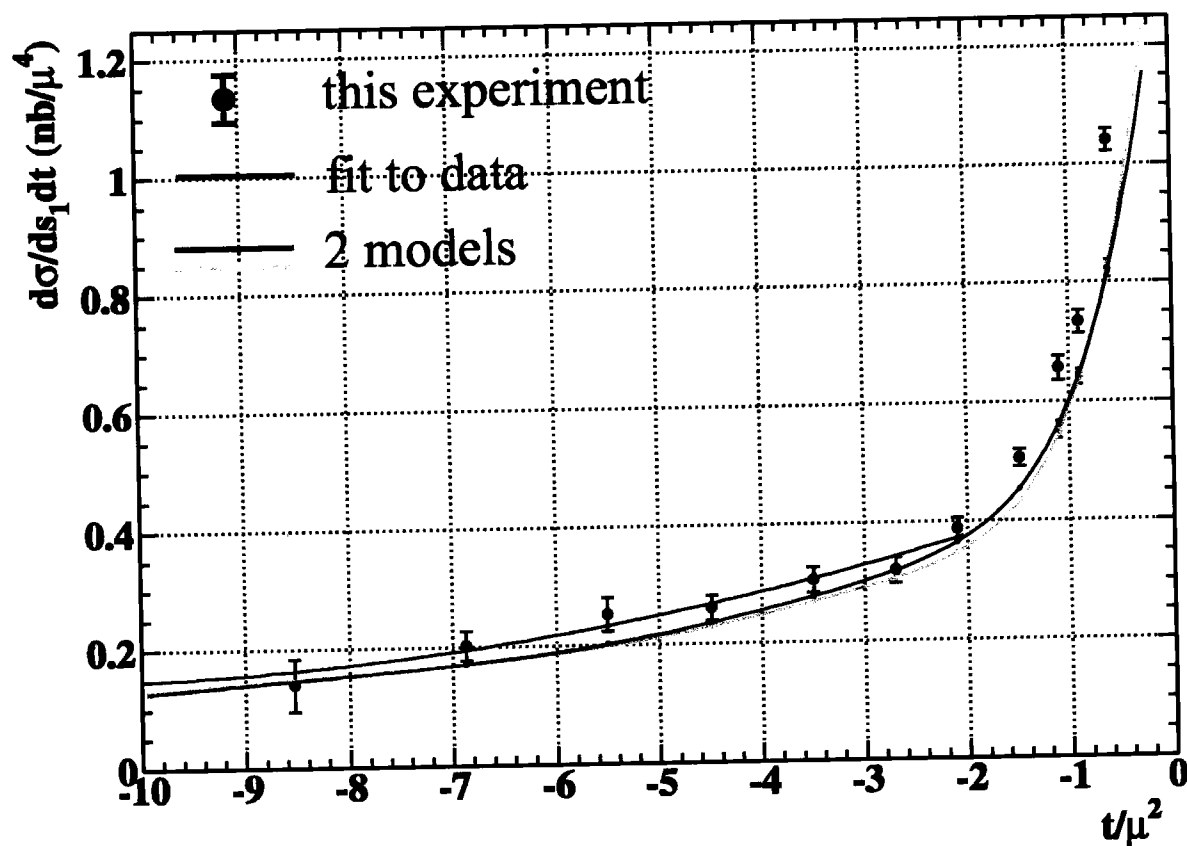


$$537 \text{ MeV} < E_\gamma < 817 \text{ MeV}$$

$$140^\circ < \theta_{\gamma\gamma'}^{\text{cm}} < 180^\circ$$

$$1.5 \mu^2 < s_1 < 5 \mu^2$$

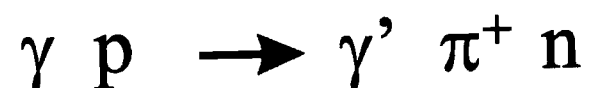
Inensitive to pion polarizability!



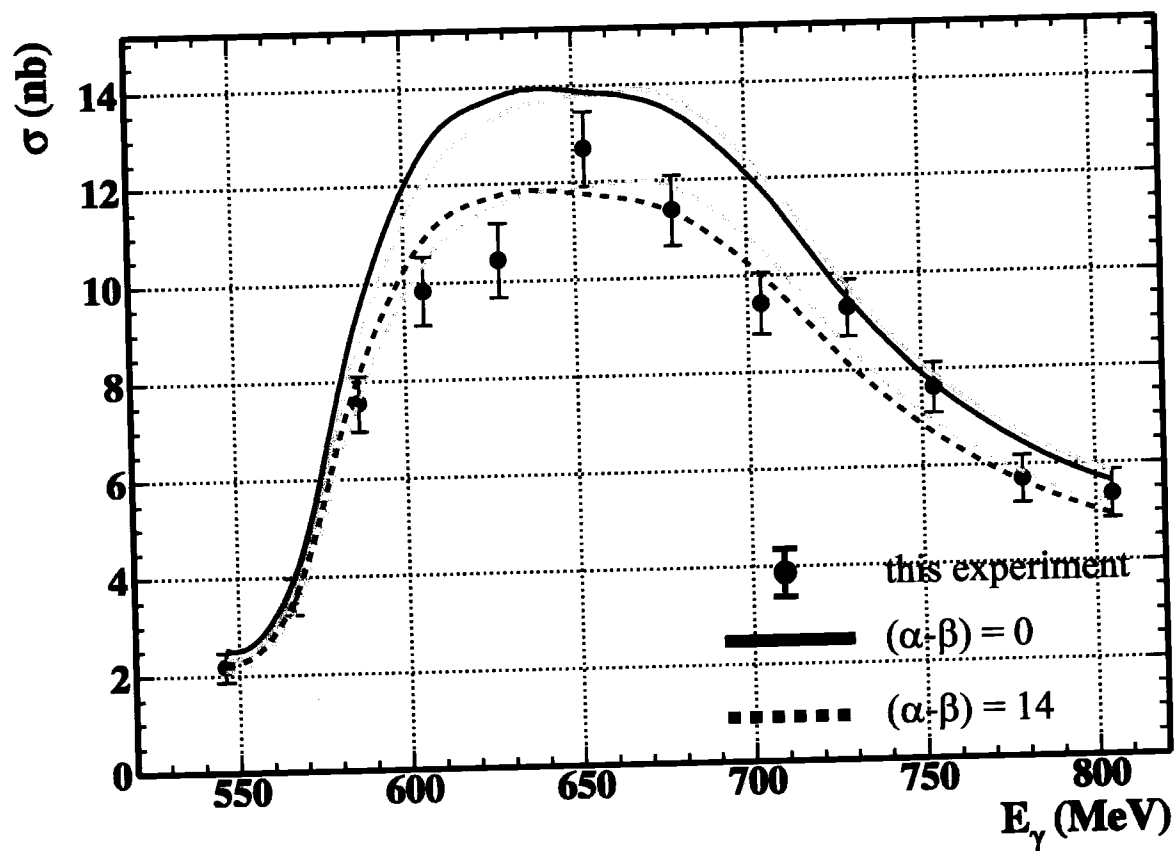




# Pion Polarizability



cross section for:  $140^\circ < \theta_{\gamma'}^{\text{cm}} < 180^\circ$   
 $-12 \mu^2 < t < -2 \mu^2$   
 $5 \mu^2 < s_1 < 15 \mu^2$



Model 1: Ufnalov

Model 2: Fil'kov

$$(\alpha-\beta) = (12.2 \pm 6.3) \times 10^{-4} \text{ fm}^3$$
$$(\alpha-\beta) = (11.1 \pm 1.4 \pm 2.8) \times 10^{-4} \text{ fm}^3$$

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## Conclusions

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Final result for pion polarizability  $(\alpha - \beta)_{\pi^+}$ :

$$(\alpha - \beta)_{\pi^+} = (11.6 \pm 1.5_{stat} \pm 3.0_{syst} \pm 0.5_{model}) \times 10^{-4} \text{fm}^3$$

deviates by 2 standard deviations from the

Chiral Perturbation Theory result;

significant deviation, but a real problem?

Explanations:

- “off-shell-pion”

the initial pion is virtual, the final is the asymptotic pion

replace point like initial pion by form factor  $\curvearrowright$  discrepancy increases

- Chiral Perturbation Theory fails

expansion for small external momenta, but how small?

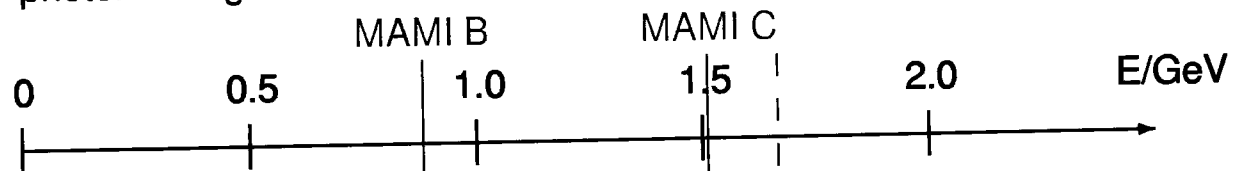
deviations manifest if  $\lambda_{\pi} \gtrsim \lambda_{\gamma^*}$ , i.e. if spatial size of pion is resolved

- modification of pion cloud picture

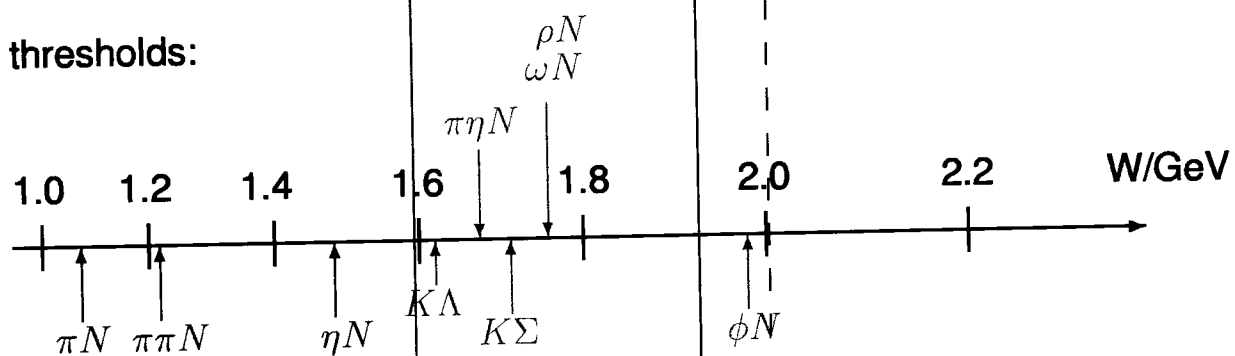
pion cloud  $\equiv$  transitional layer between superconductor (QCD vacuum) and normal conductor (interior of hadron, confined quarks and gluons)?

# ranges of physics

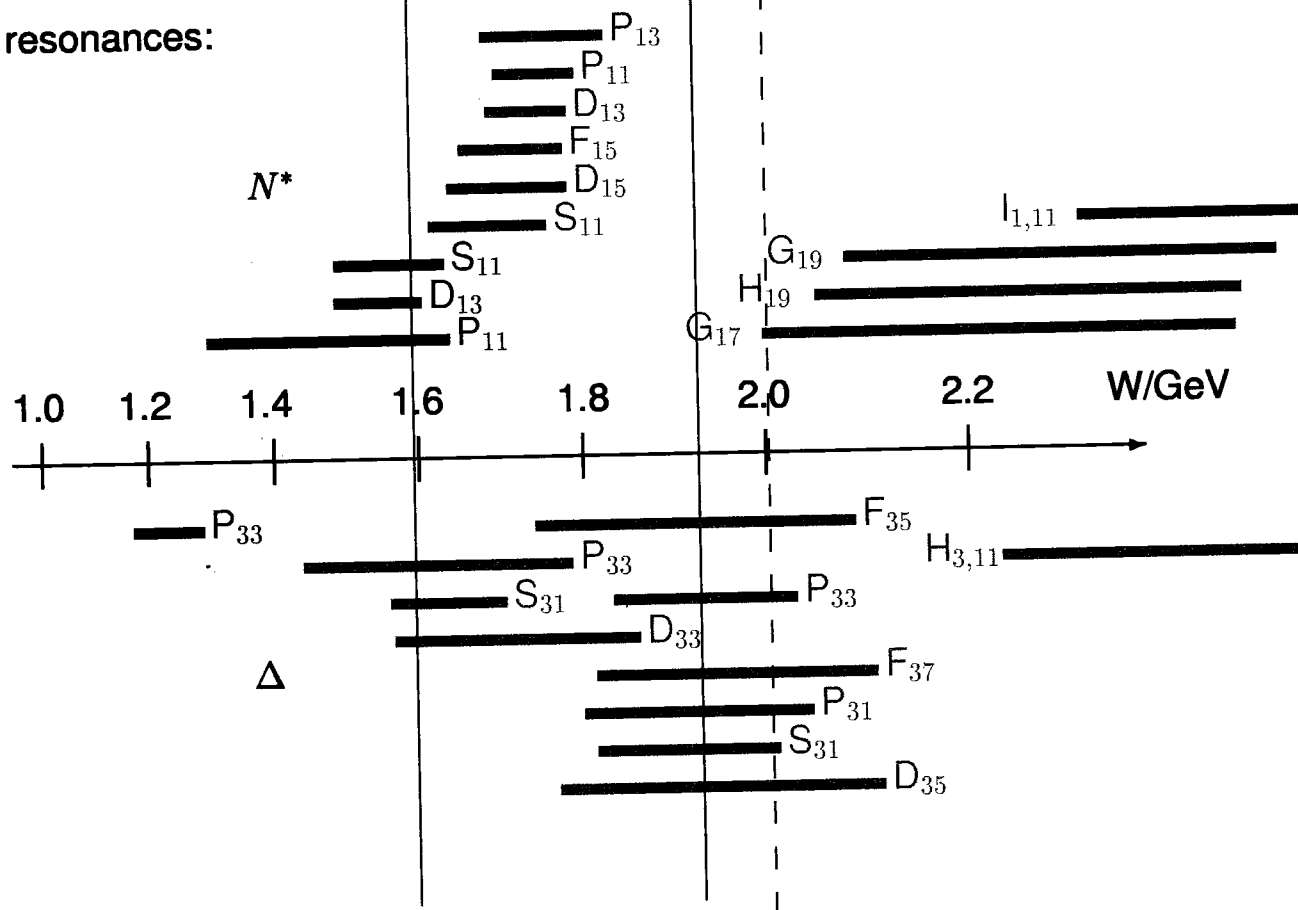
photon energies:



thresholds:



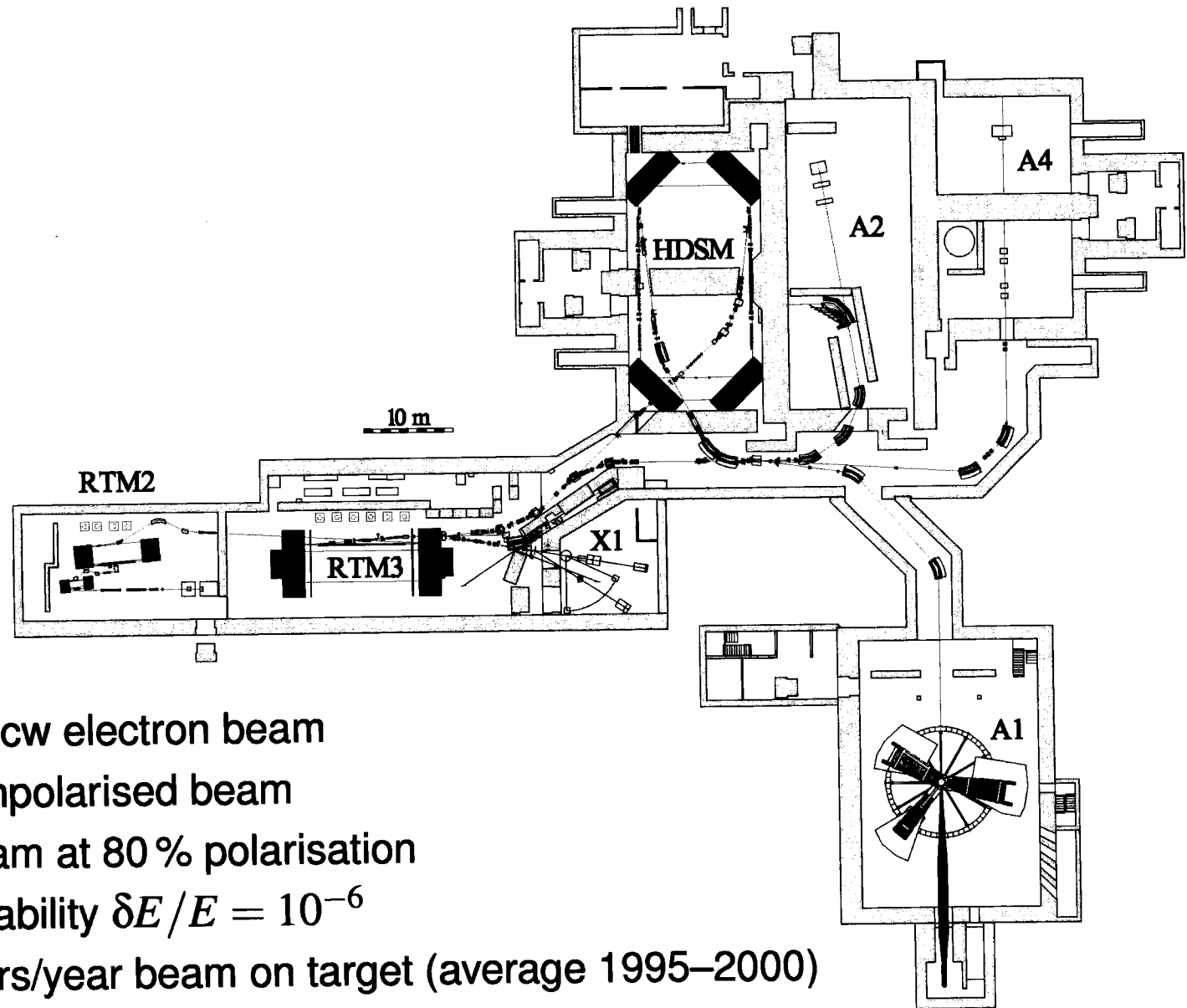
resonances:



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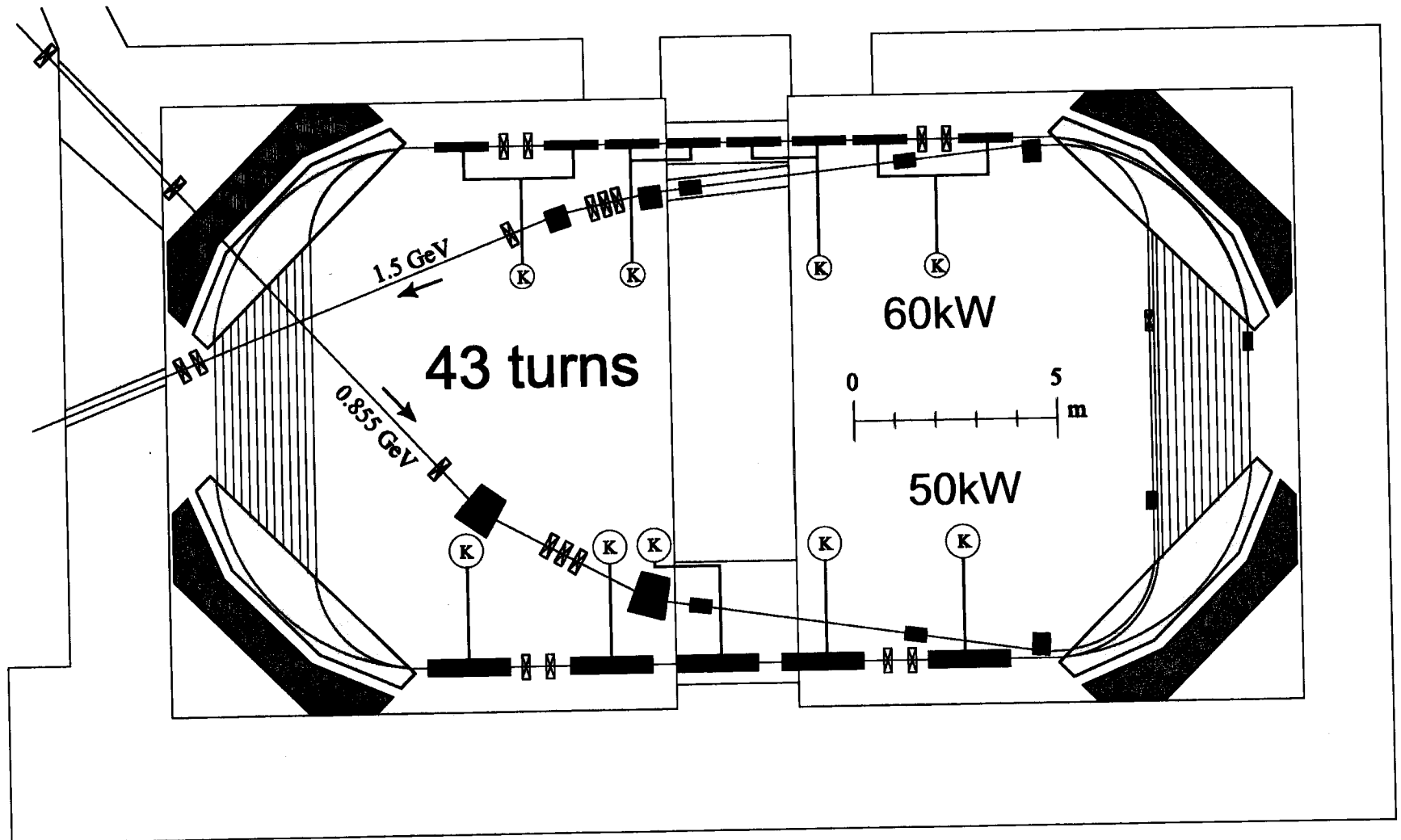
## The MAMI accelerator

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- 855 MeV cw electron beam
- $100\ \mu\text{A}$  unpolarised beam
- $30\ \mu\text{A}$  beam at 80 % polarisation
- energy stability  $\delta E/E = 10^{-6}$
- 5500 hours/year beam on target (average 1995–2000)

# MAMI C



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## MAMI collaborations and their experimental equipment

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- **A1 collaboration**

- ★ 3-Spectrometer-Set-up
- ★  $\pi$  Short Orbit Spectrometer
- ★ neutron polarimeter and detectors
- ★  ${}^3\vec{He}$  target
- ★ KAOS Kaon short orbit Spectrometer

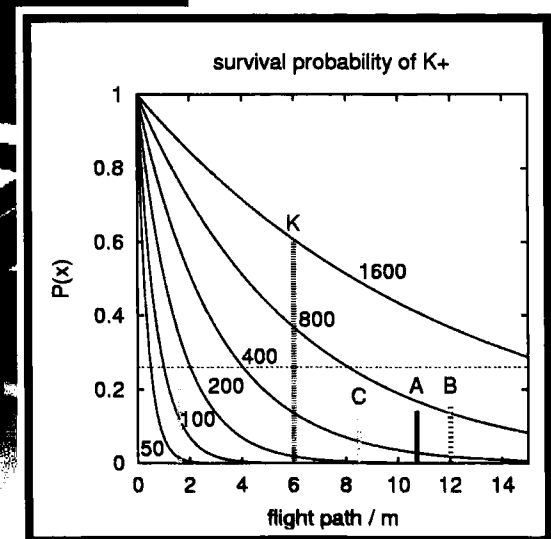
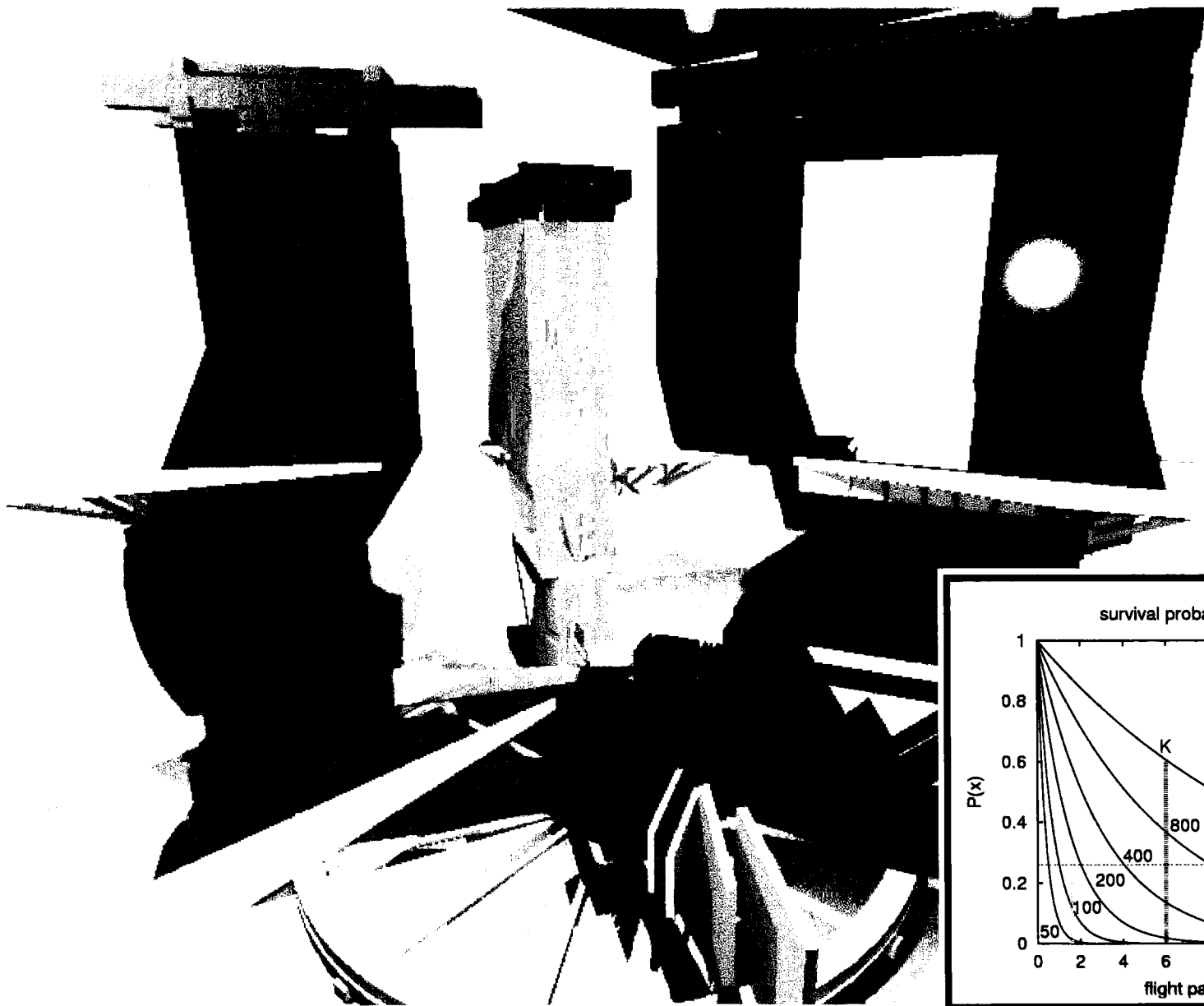
- **A2 collaboration**

- ★ Photon-Tagger
- ★ DAPHNE, TAPS, etc.
- ★ Crystal Ball
- ★  $\vec{p}$  target

- **A4 collaboration**

- ★ granulated Cherenkov detector
- ★ high power  $LH_2$  target

# KAOS @ A1



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## Crystal Ball and TAPS at MAMI

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TAPS

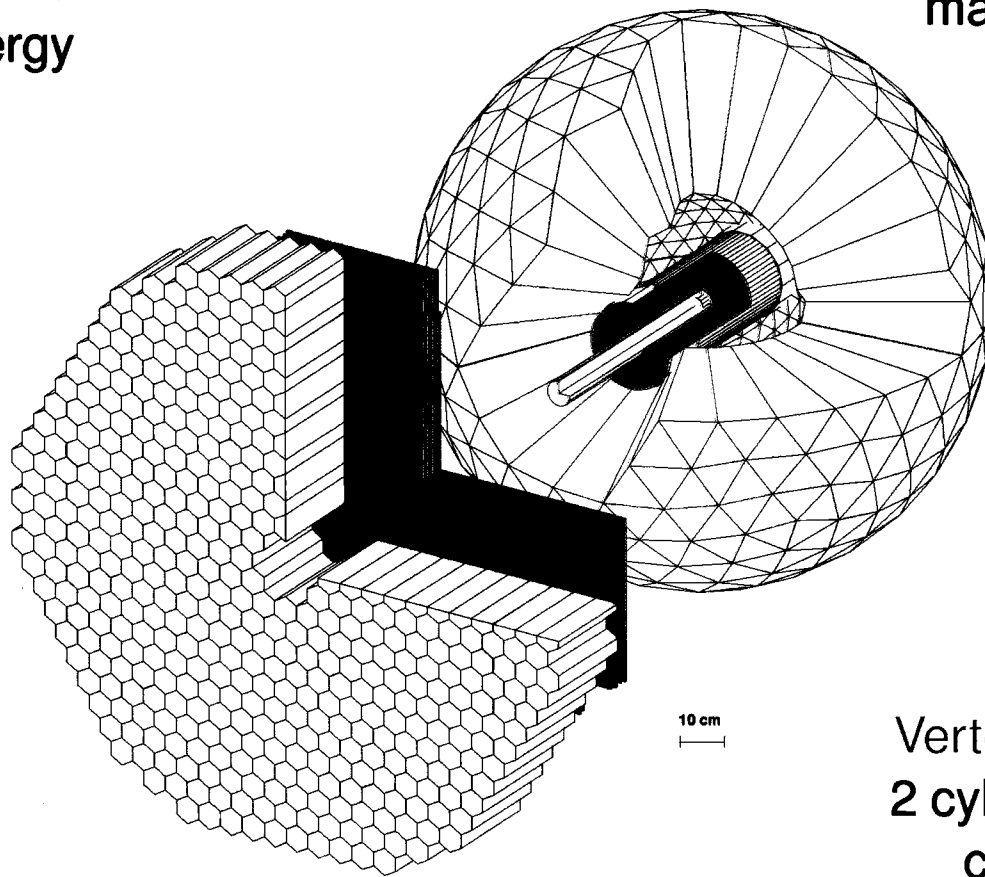
510 BaF<sub>2</sub> detectors

max. kinetic energy

$\pi^\pm$  : 180 MeV

$K^\pm$  : 280 MeV

$p$  : 360 MeV



Crystal Ball

672 NaJ detectors

max. kinetic energy

$\mu^\pm$  : 233 MeV

$\pi^\pm$  : 240 MeV

$K^\pm$  : 341 MeV

$p$  : 425 MeV

Vertex detectors

2 cylindrical wire  
chambers

480 wires, 320 strips

24 thin plastic counters

particle identification



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## Physics Program at MAMI

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- MAMI B ( $180 \text{ MeV} < E < 885 \text{ MeV}$ ) : from 1992 to 2005 and beyond
- MAMI C ( $180 \text{ MeV} < E \lesssim 1500 \text{ MeV}$ ) : starting 2005

### 1. Structure of the Nucleon

- form factors  $G_E^p, G_E^n, G_A$
- polarizabilities at  $Q^2 = 0$  and  $Q^2 > 0$
- spin structure
- nucleon resonances in selective decay channels
  - ★  $\gamma p \rightarrow \Delta \gamma_{\text{internal decay}} \rightarrow p \pi^0 \gamma \rightsquigarrow$  magnetic moment of  $\Delta(1232)$
  - ★ Roper resonance

### 2. Mesonic Structure of the Nucleon

- threshold production of mesons  $\pi, 2\pi, \eta, \pi\eta, 2\eta, \rho, \omega, \dots$
- structure of mesons: formfactors, polarizabilities
- mesonproduction in the region of the resonances

### 3. Strange Hadrons - Strangeness in Strongly Interacting Systems

- strange meson production at threshold: chiral dynamics
- $K^0$  formfactors
- hyperons: formfactors, polarization, resonances
- hypernuclei: momentum distribution of  $\Lambda$  in the nucleus, separated L/T structure functions

### 4. Parity Violation in Electron Scattering

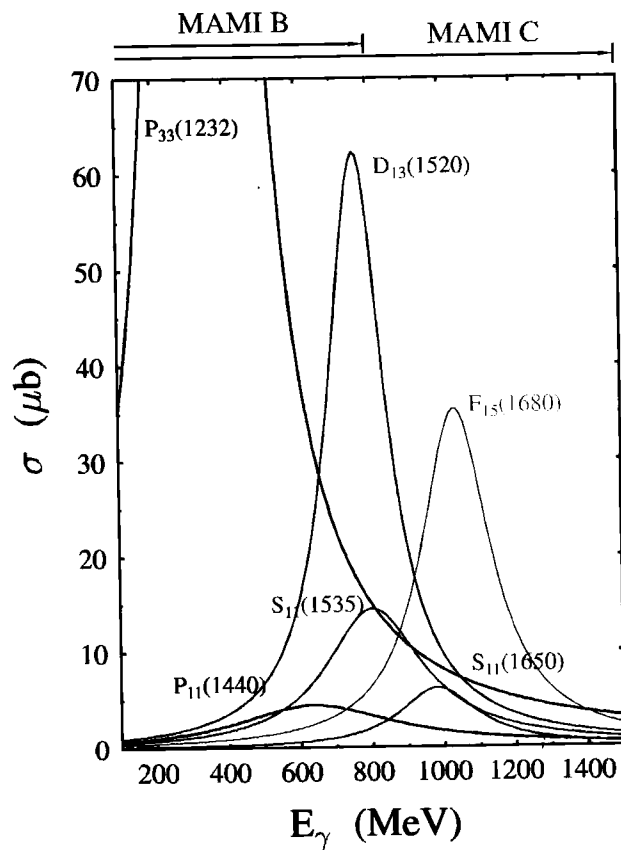
- electric and magnetic flavour singlet form factors: strangeness in proton and neutron
- transverse polarization  $\curvearrowright$  two photon exchange

### 5. Few Nucleon Systems

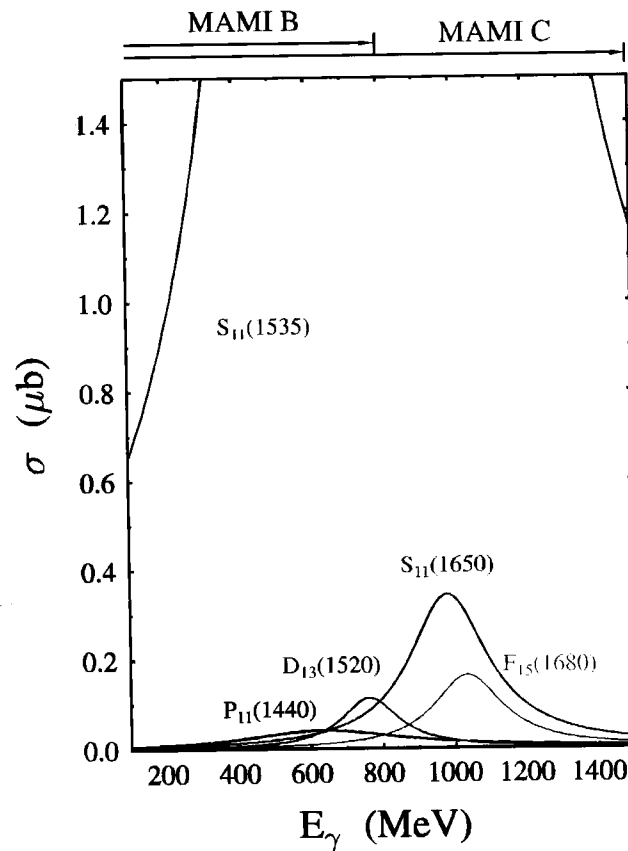
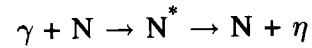
- structure of few nucleon systems: wave functions, MEC, RC, BC, ...
- GDH sum rule in few nucleon systems
- $E2/M1$  ratio for bound nucleons
- mesons in the nuclear medium

# Nucleon Resonances

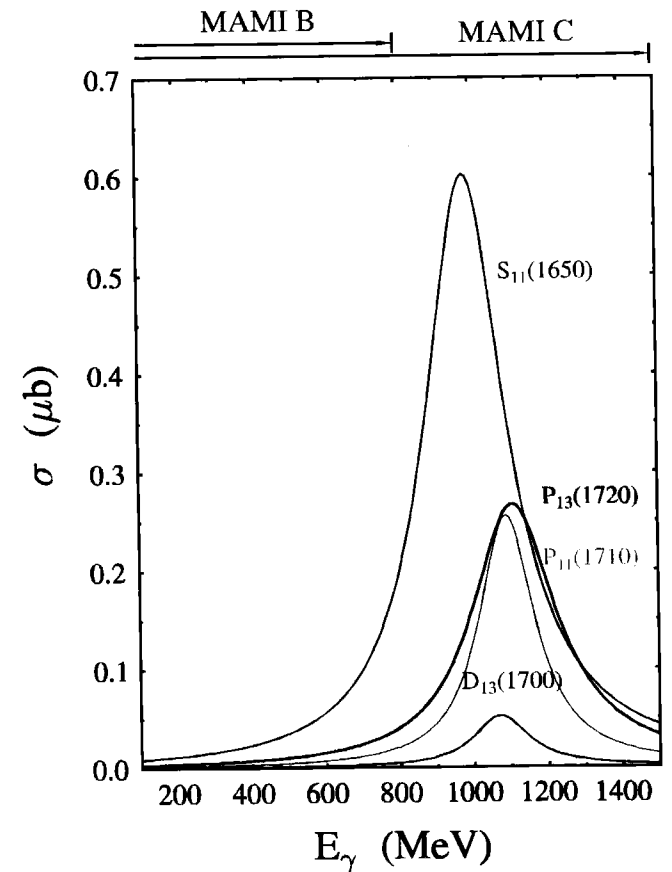
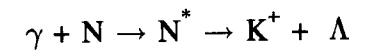
pion production



eta production



kaon production



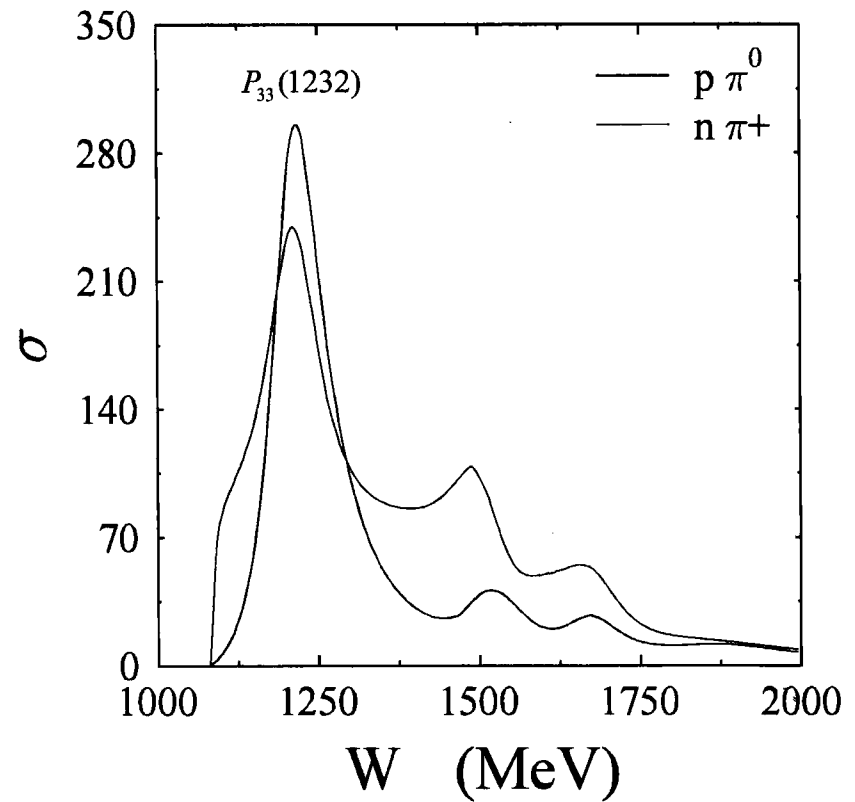
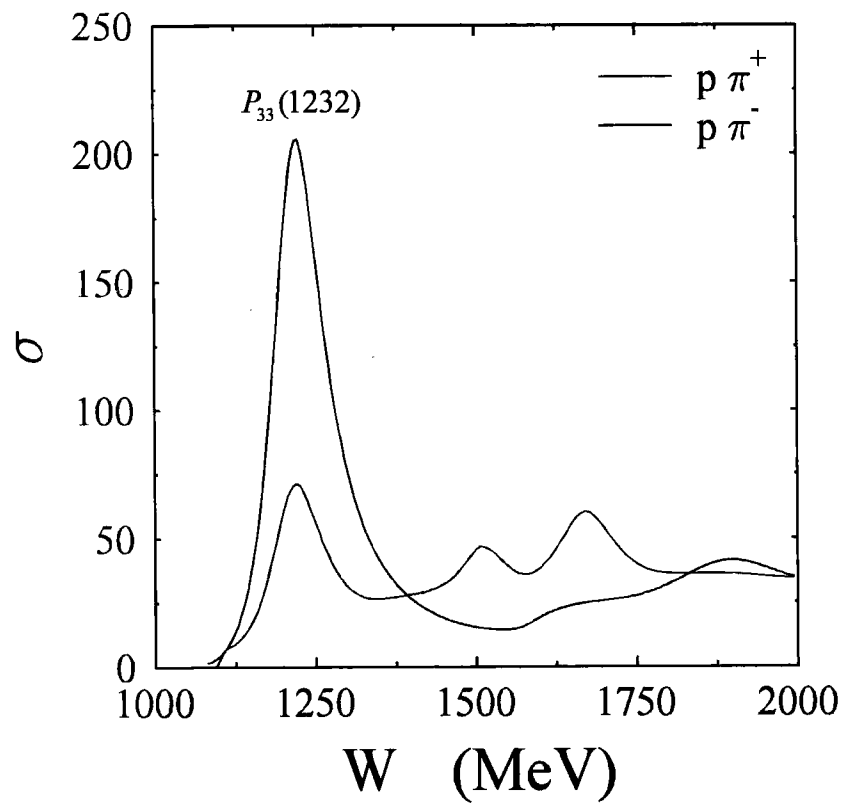
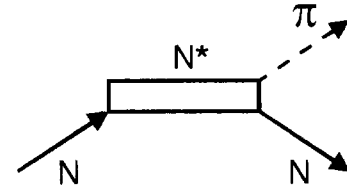
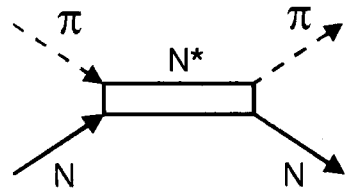
Problem : overlapping resonances

Solution : polarization observables

MAMI C : polarized photons, polarized targets  
and recoil-proton polarimeter

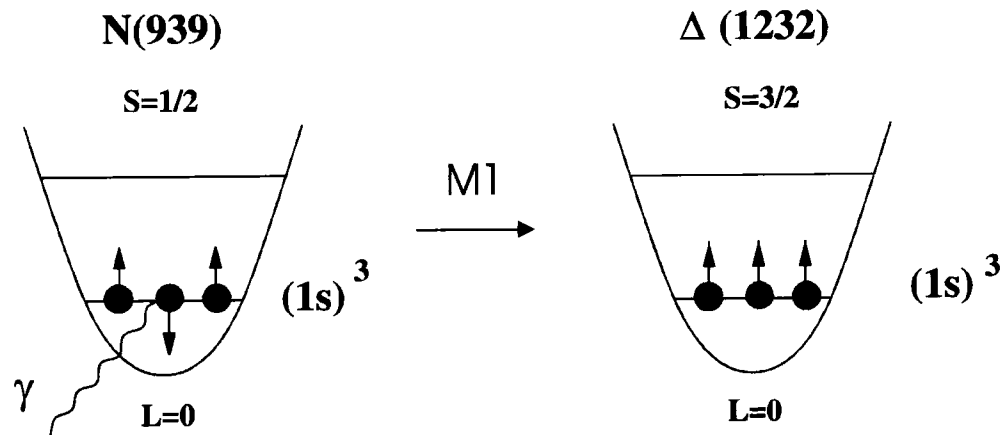
# Nucleon Resonance

1951 E. Fermi :  $\pi^+ + p \rightarrow p + \pi^+$  discovery of the first nucleon resonance  $P_{33}(1232)$



# $\Delta^+$ (1232) Resonance

$\Delta^+$  (1232) resonance nucleon first excited state

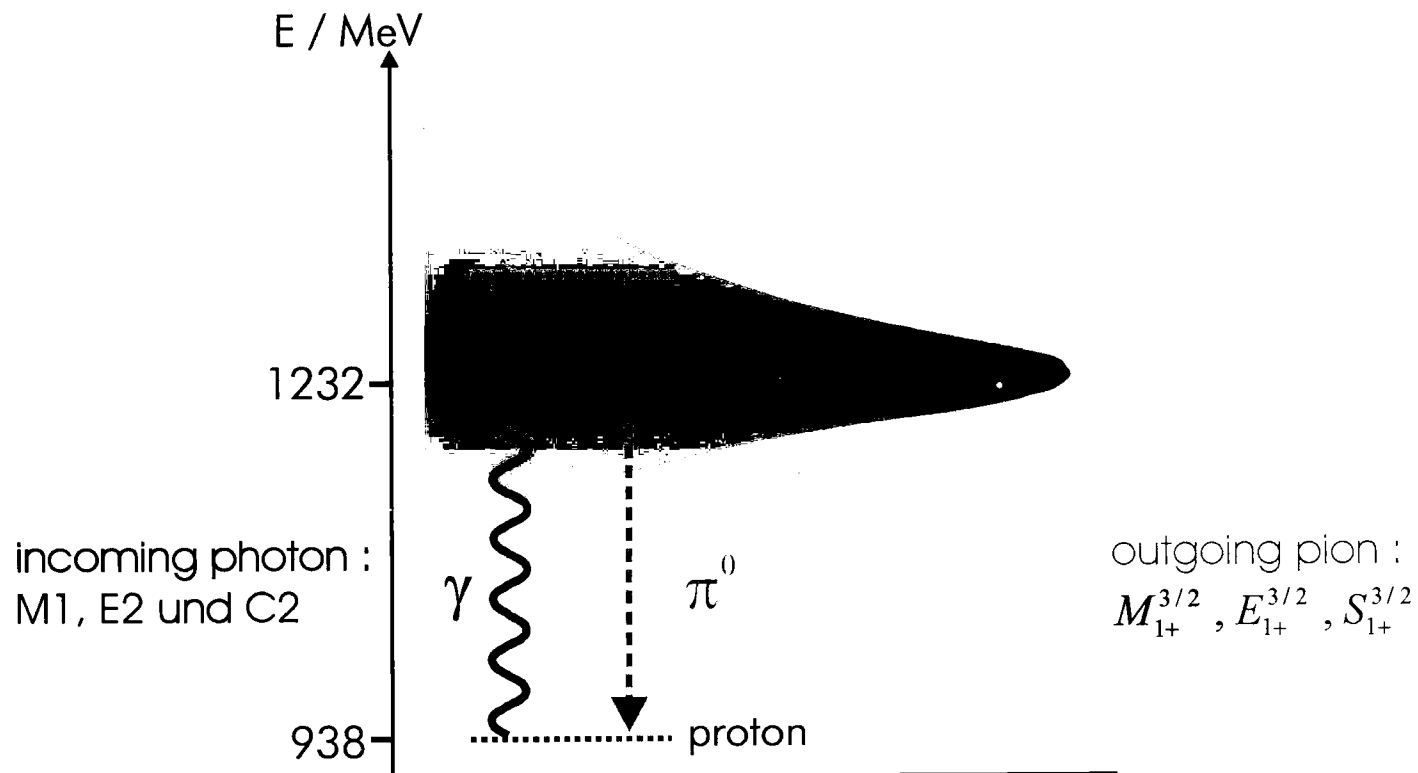


precise electro- and photoproduction data :  $\gamma + p \rightarrow \Delta^+ \rightarrow \pi^0 + p$

magnetic dipole transition M1

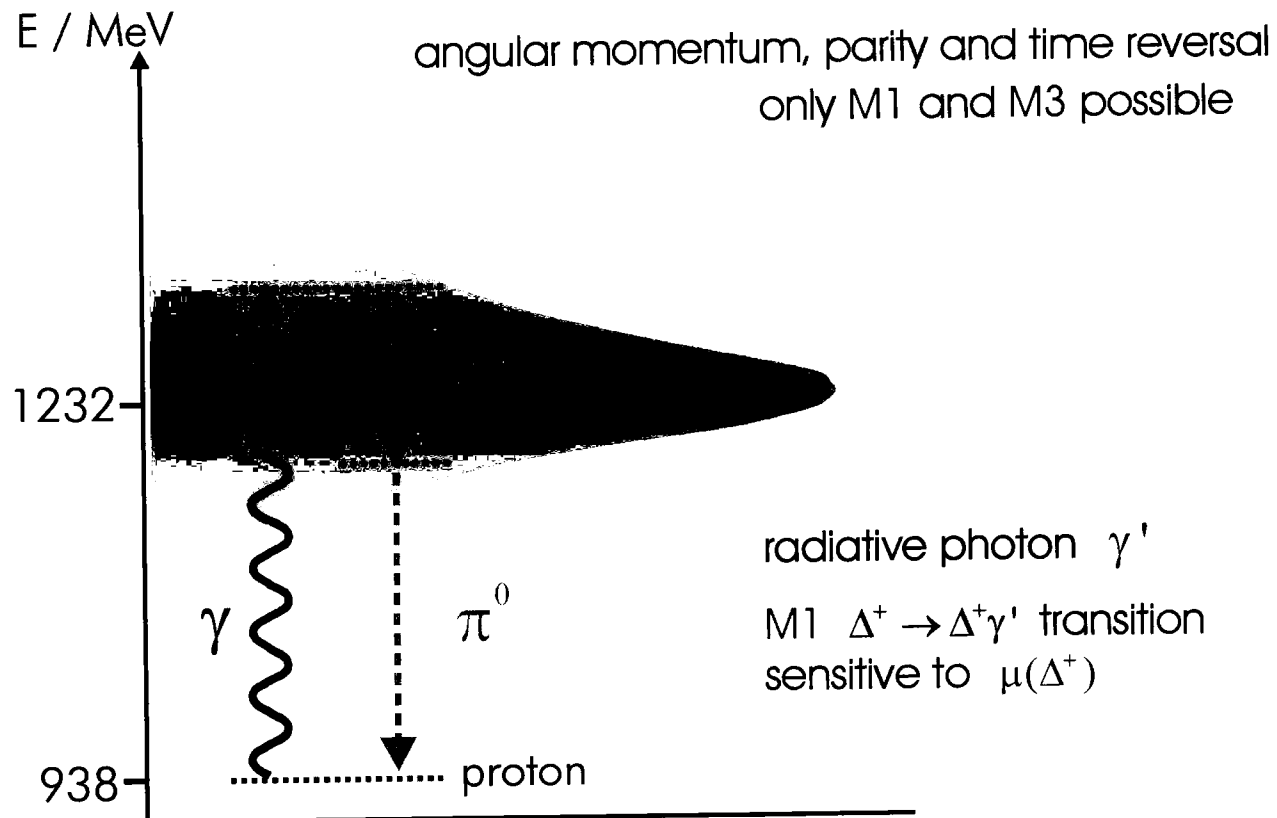
electric quadrupole transition E2

Coulomb quadrupole transition C2

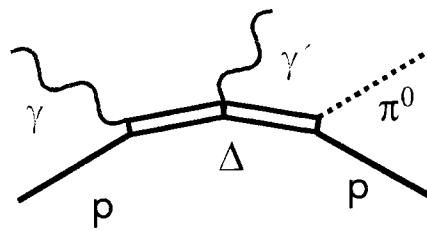


# $\Delta^+$ (1232) Magnetic Moment

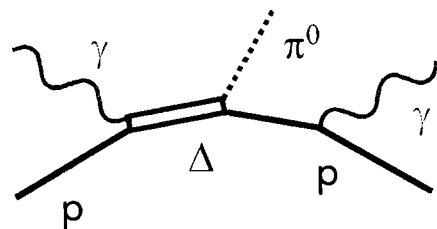
radiative pion photoproduction:  $\gamma + p \rightarrow \Delta^+ + \gamma' \rightarrow \pi^0 + p + \gamma'$



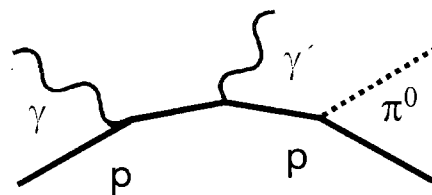
$\Delta$  excitation and identification of the  $p\pi^0\gamma'$  final state



Problem :  
Proton bremsstrahlung



Nonresonant contributions small in  $\Delta$ -resonance region



# 16 Polarization Observables in Meson Photoproduction

Photon		Target	Recoil	Target-Recoil
		$x \quad y \quad z$	$x' \quad y' \quad z'$	$x' \quad x' \quad z' \quad z'$ $x \quad z \quad x \quad z$
unpolarized	$\sigma$	$0 \quad T \quad 0$	$0 \quad P \quad 0$	$T_{x'} \quad -L_{x'} \quad T_{z'} \quad L_{z'}$
linearly polarized	$-\Sigma$	$H \quad (-P) \quad -G$	$O_{x'} \quad (-T) \quad O_{z'}$	$(-L_{z'}) \quad (T_{z'}) \quad (-L_{x'}) \quad (-T_{x'})$
circularly polarized	$0$	$F \quad 0 \quad -E$	$-C_{x'} \quad 0 \quad -C_{z'}$	$0 \quad 0 \quad 0 \quad 0$

good experimental  
results only for :

$$\sigma, \Sigma, T, E$$

Observable G  
sensitive to  $P_{11}(1440)$

$$\vec{\gamma} \vec{p} \rightarrow p \pi^0$$

Kaon threshold  
production

$$\vec{\gamma} p \rightarrow K^0 \bar{\Sigma}^+ \quad \bar{\Sigma}^+ \rightarrow p \pi^0 \text{ self analyzing}$$

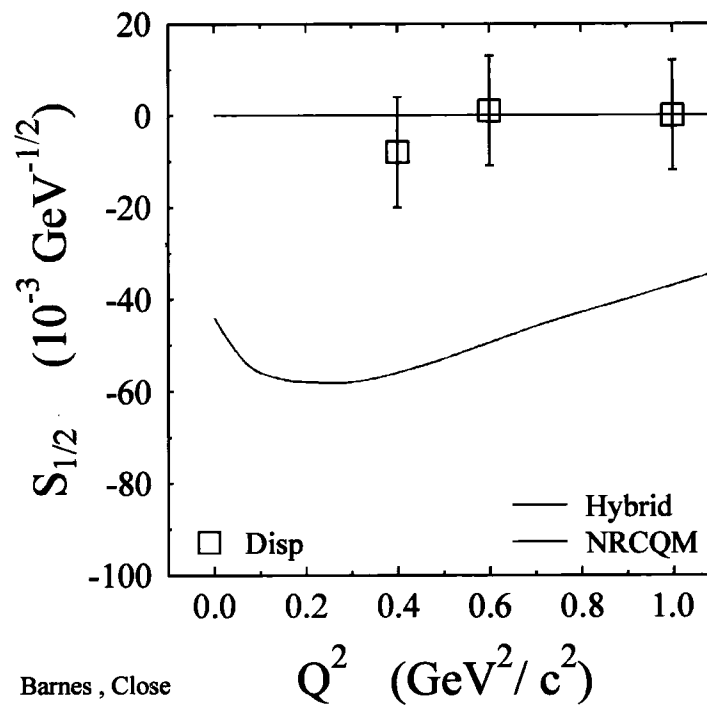
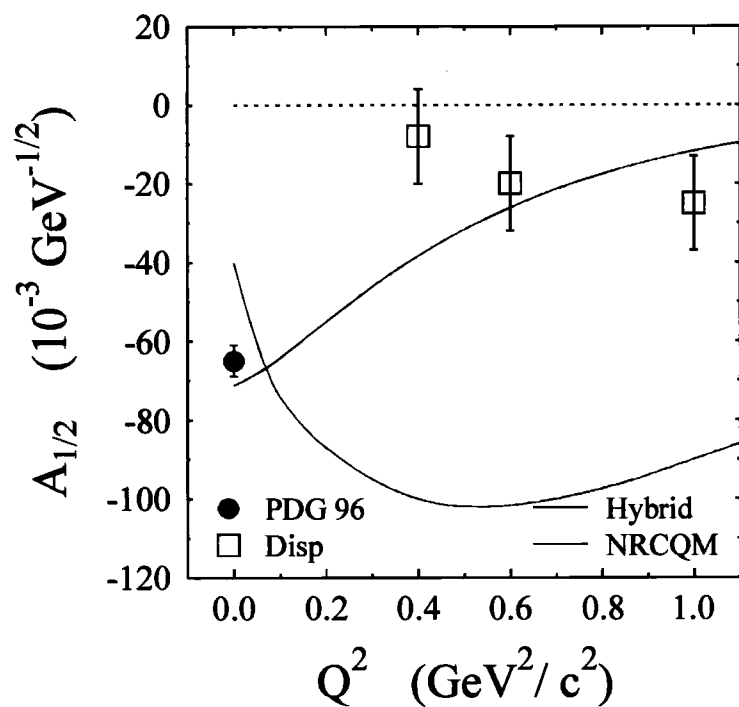
Observable E  
sensitive to GDH sum rule

# Roper Resonance

quark picture :  $P_{11}(1440)$  radial excitation

- problems :
- $M \approx 1440 \text{ MeV}$   $\Gamma \approx 350 \text{ MeV}$
  - helicity amplitudes  $A_{1/2}$  and  $S_{1/2}$   
absolute value and sign
  - $Q^2$  dependence of  $A_{1/2}$  and  $S_{1/2}$

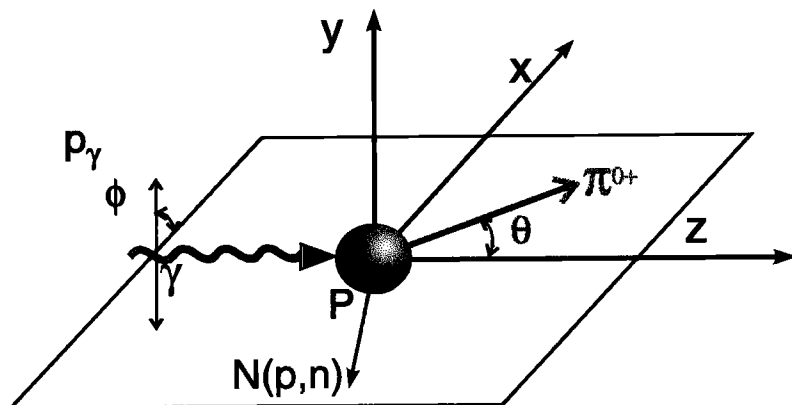
- proposed solutions :
- not a  $|3q\rangle$  excitation
  - hybrid  $|3q g\rangle$
  - $N\sigma$  molecule
  - two resonances



Barnes, Close  
Li, Burkert



# The Double Polarization Observable G



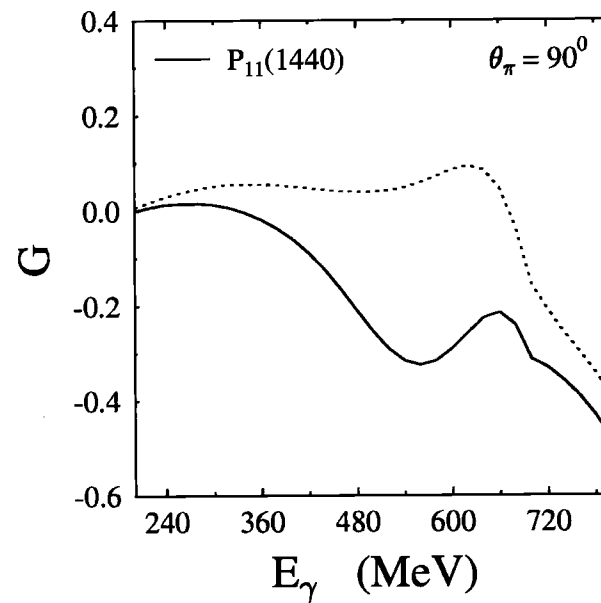
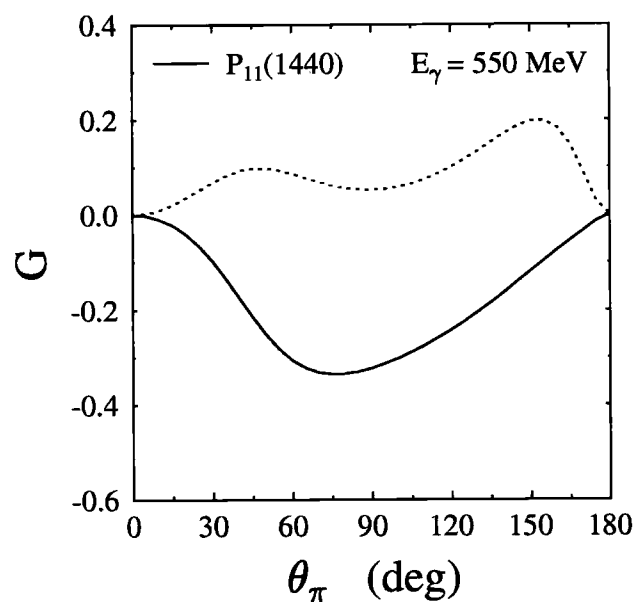
$$\vec{\gamma} + \vec{p} \rightarrow N + \pi = \begin{cases} n + \pi^+ \\ p + \pi^0 \end{cases}$$

$\vec{\gamma}$  : linearly polarized photons

$\vec{p}$  : longitudinally polarized protons

$$\frac{d\sigma}{d\Omega}(\phi, \theta) = \frac{d\sigma}{d\Omega}(\theta) \left\{ 1 - p_\gamma \Sigma \cos(2\phi) + p_\gamma p_z G \sin(2\phi) \right\}$$

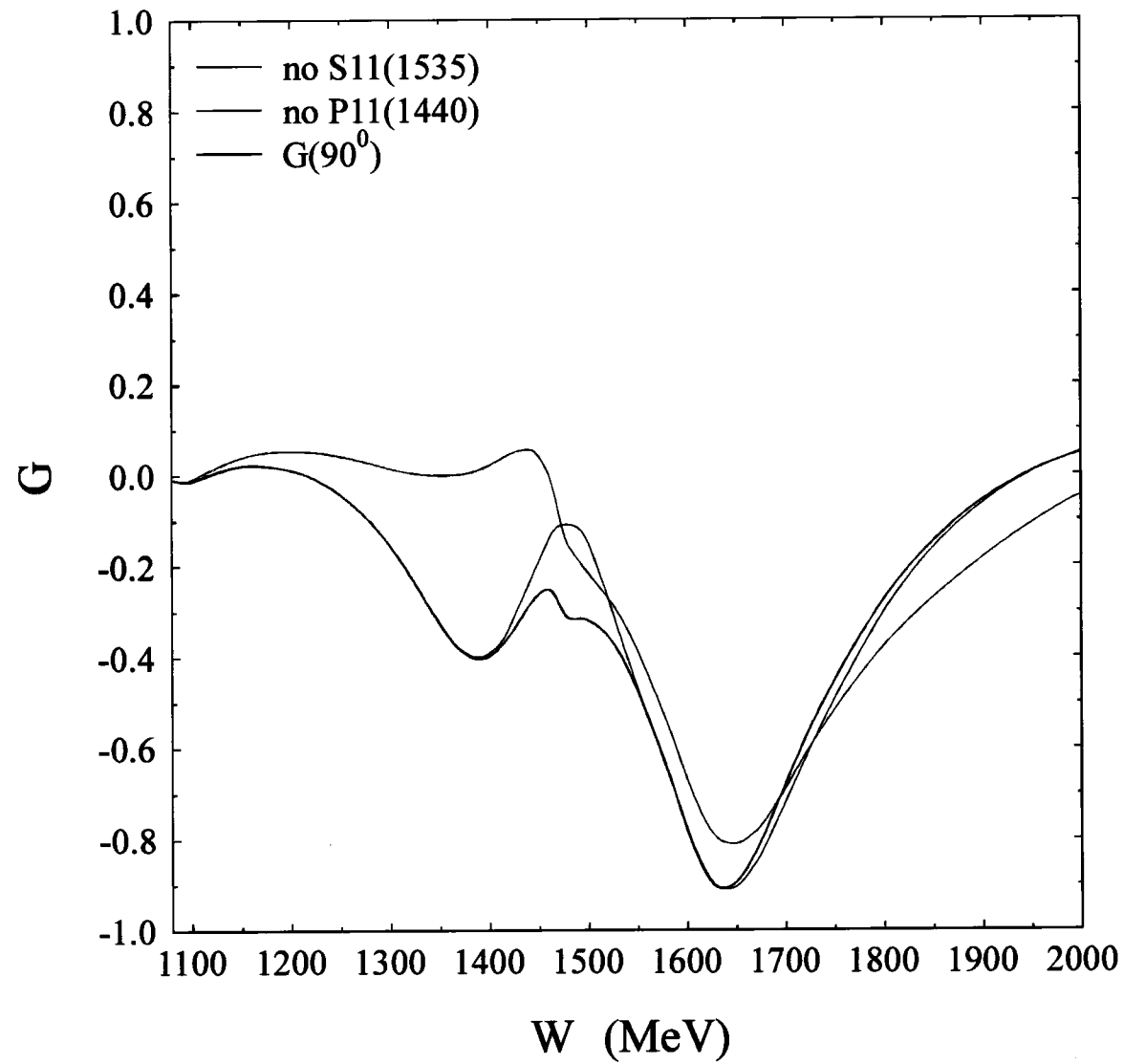
$$G \sim \text{Im}M_{1-} - \text{Re}M_{1+}$$



# Roper Resonance

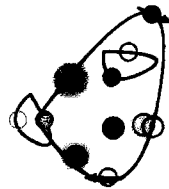
$$\vec{\gamma} \vec{p} \rightarrow p \pi^0$$

Asymmetry G



Crystal Ball @ MAMI C

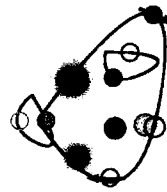




SFB 443

## Conclusions I

- Mainz Microtron MAMI produces significant information about hadrons
  - \* form factors of the nucleon  $G_{E,p}, G_{E,n}, G_{M,p}, G_{M,n}$   
2% effect at the  $\pi$  wavelength or larger in  $G_{E,p}, G_{E,n}, G_{M,p}, G_{M,n}$
  - \* pion polarizability  $(\alpha - \beta)_{\pi^+}$   
2 standard deviations from ChPTh ( $\chi P\Theta$ ) calculations  
nature of  $\pi$  cloud?
  - \* pion photoproduction  $p(\gamma, \pi^0)p, p(\vec{\gamma}, \pi^0)p$   
good agreement with ChPTh at  $Q^2 = 0$
  - \* pion electroproduction  $p(e, e'p)\pi^0, p(\vec{e}, e'p)\pi^0$   
less good agreement with ChPTh at  $Q^2 > 0$
  - \* helicity dependent photo production  $p(\vec{\gamma}, \{\pi^+, \pi^0, 2\pi\})p$   
reasonable agreement with effective models for  $\pi^+, \pi^0$
  - \* weak form factors  $p(\vec{e}, e)p$   
first results about strangeness content of nucleon published  
experiments in broader kinematical range in progress



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## Conclusions II

- Significant hadron observables and methods promising connections to non perturbative QCD have emerged:
  - \* **observable:**
    - form factors and polarizabilities of baryons and mesons
    - selected resonance amplitudes below  $W < 1.9 \text{ GeV}$
    - threshold reactions ( $\gamma^*$ ,  $\{n * \pi, K, \eta, \omega, \rho, \dots\}$ )
  - \* **experiment:**
    - polarization of dense targets and high intensity beams
    - detectors with large acceptance or excellent resolution
  - \* **theory:**
    - chiral perturbation theory, QCD inspired models, lattice gauge theory
- MAMI B (885 MeV) 1992 - 2004  
MAMI C (1500 MeV) 2005 - 201X